

Sources and sinks on single neurons

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Department of Theory*

The source

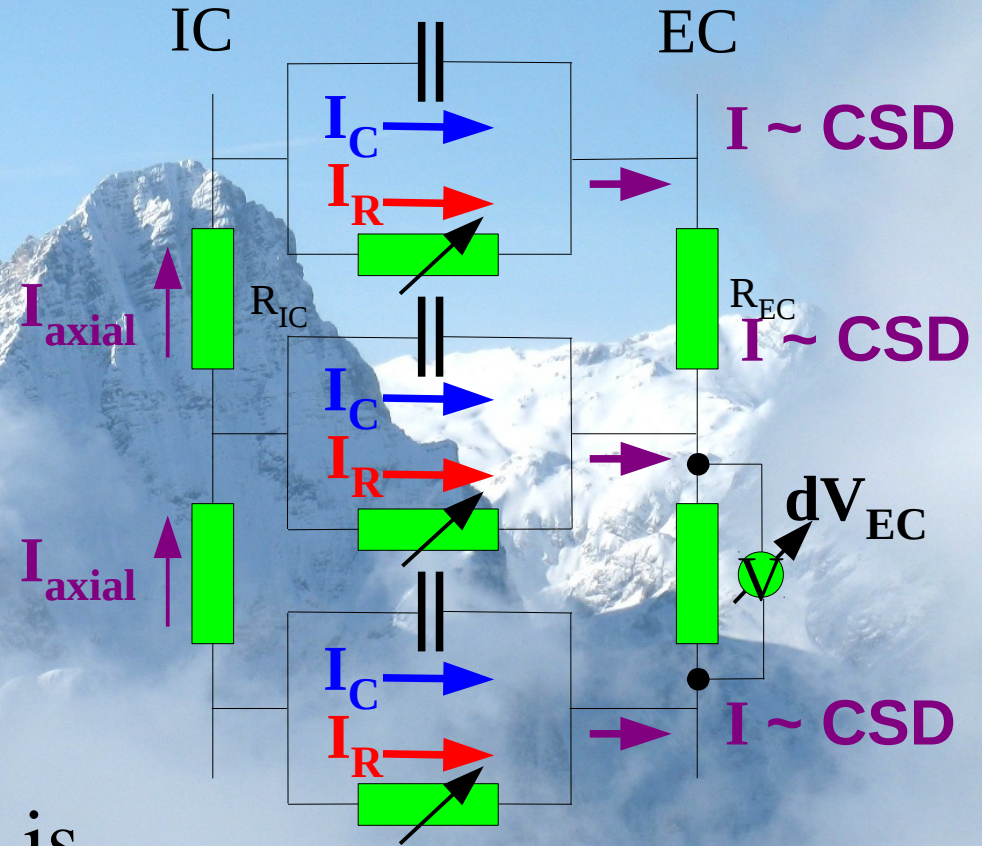
What is the source of the extracellular potential?

The membrane current!

Which membrane current?

$$I(r, t) = I_R(r, t) + I_C(r, t)$$

The source of the EC potential is the sum of the capacitive and resistive currents



The source

The capacitive current is:

$$I_C = C_m \frac{dV_m}{dt}$$

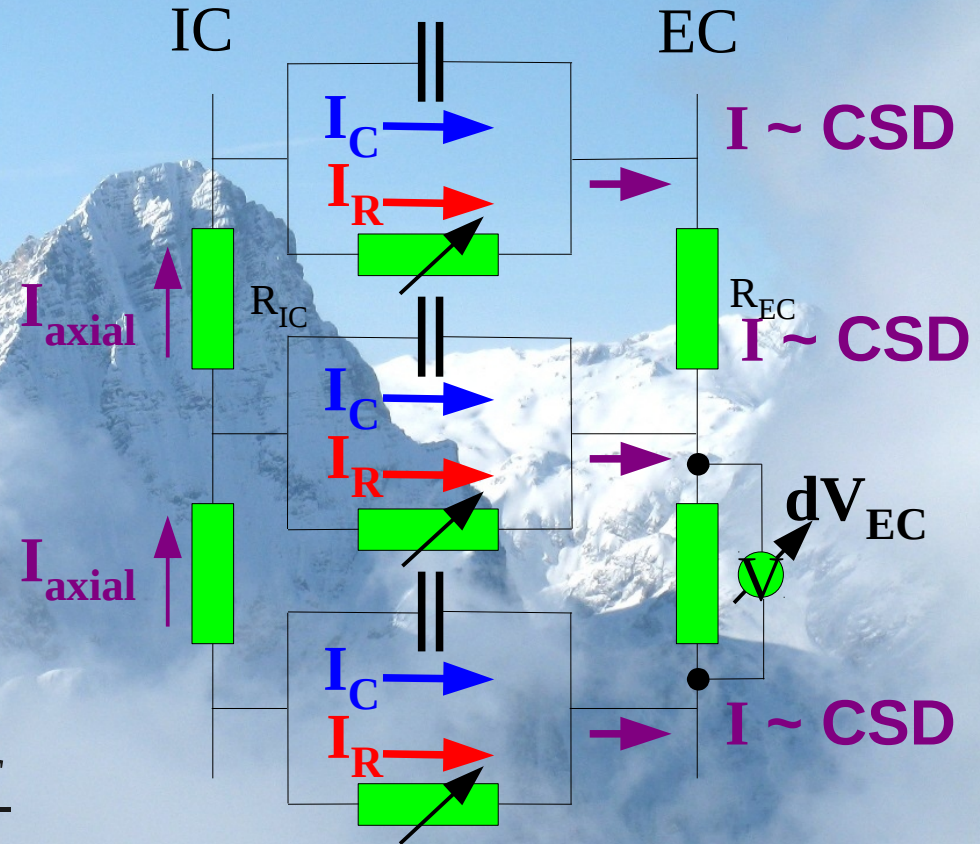
Substituting back :

$$C_m \frac{dV_m}{dt} = -I_R + I$$

Thus:

$$I = \frac{\partial I_{axial}}{\partial x} \approx \frac{\partial^2 V_m}{\partial x^2} \approx \frac{-\partial^2 V_{EC}}{\partial x^2}$$

Assuming
sealed ends: $\sum I = 0$



The source

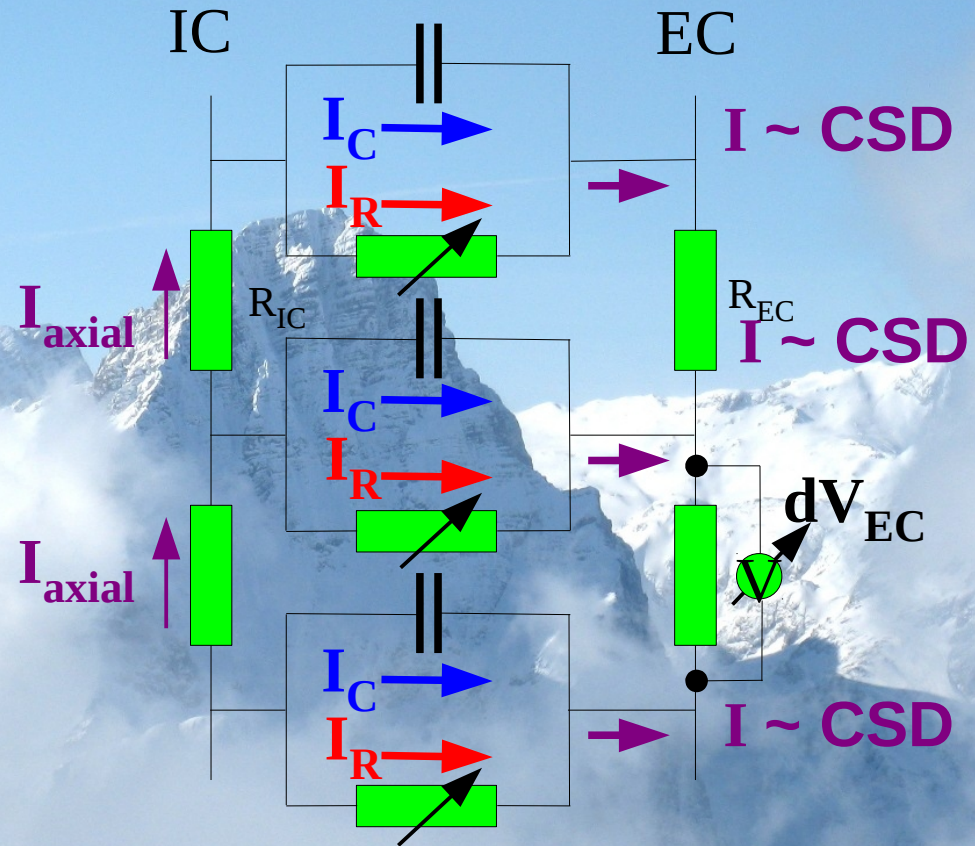
In voltage clamp:

$$C_m \frac{dV_m}{dt} = I_C = 0$$

Thus,

$$I = I_R$$

In voltage clamp, I_R is measurable, but the extracellular potential is generated by the net membrane current I not I_R



The sum of I_R is not zero, but the sum of I is zero for the whole cell!

The rule

Generation of the extracellular potential patterns is governed by the Poisson equation:

$$\nabla^2 V(r) = \frac{\partial^2 V(r)}{\partial x^2} + \frac{\partial^2 V(r)}{\partial y^2} + \frac{\partial^2 V(r)}{\partial z^2} = \frac{-I(r)}{\sigma_e}$$

The forward problem:

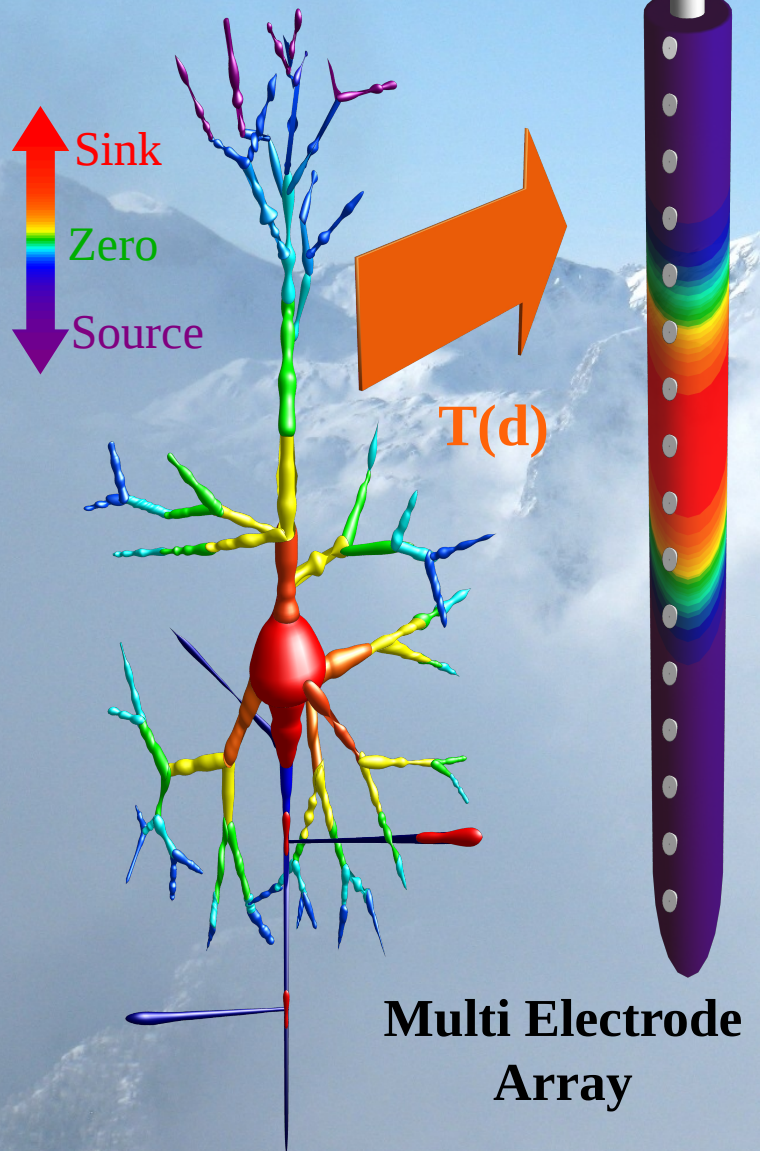
Calculating V while I is known: modelling

The inverse problem:

Calculating I while V is known: analysis

The forward problem

Original current source density distribution



The Green-function method provides the solution.

The discretised form:

$$V_i = \frac{1}{4\pi\sigma_e} \sum_{j=1}^N \frac{I_j}{|\mathbf{r}_i - \mathbf{r}_j|}$$

In matrix formalism:

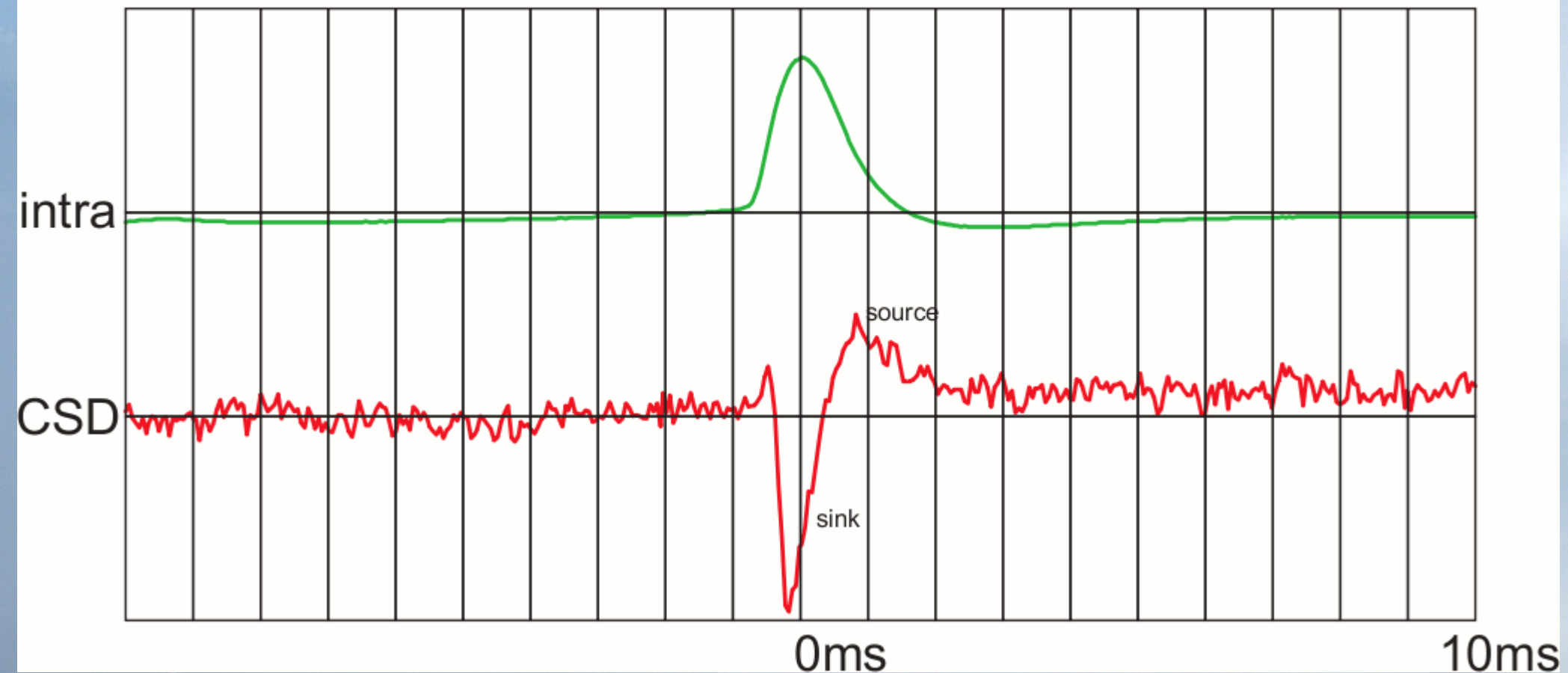
$$\mathbf{V} = \mathbf{T} \mathbf{I}$$

In case of a linear probe and cell \mathbf{T} can be calculated as:

$$T_{ij} = \frac{1}{4\pi\sigma_e} \frac{1}{\sqrt{(x_i - x_j)^2 + d^2}}$$

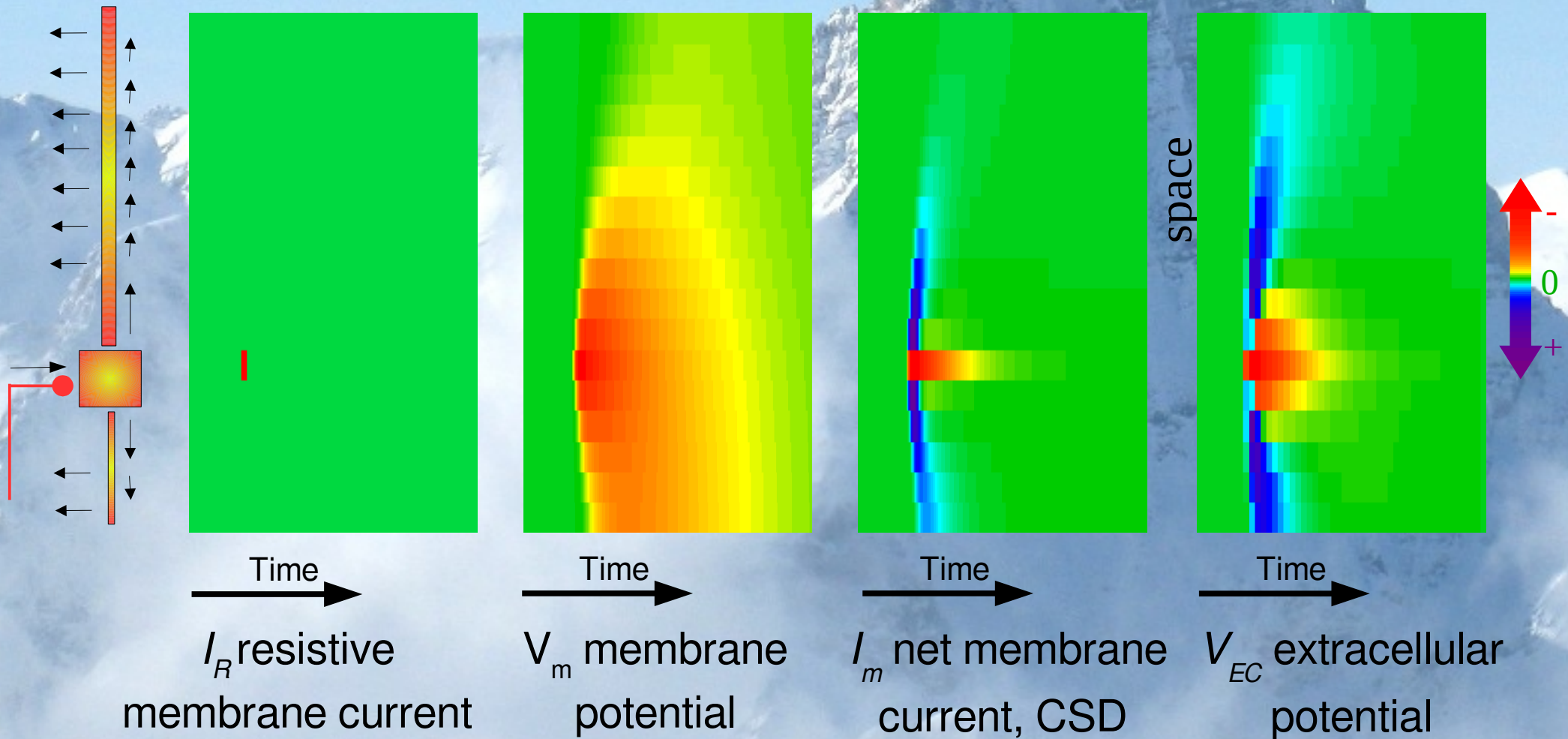
Parallel EC and IC recordings in a hippocampal slice

Intra vs. CSD



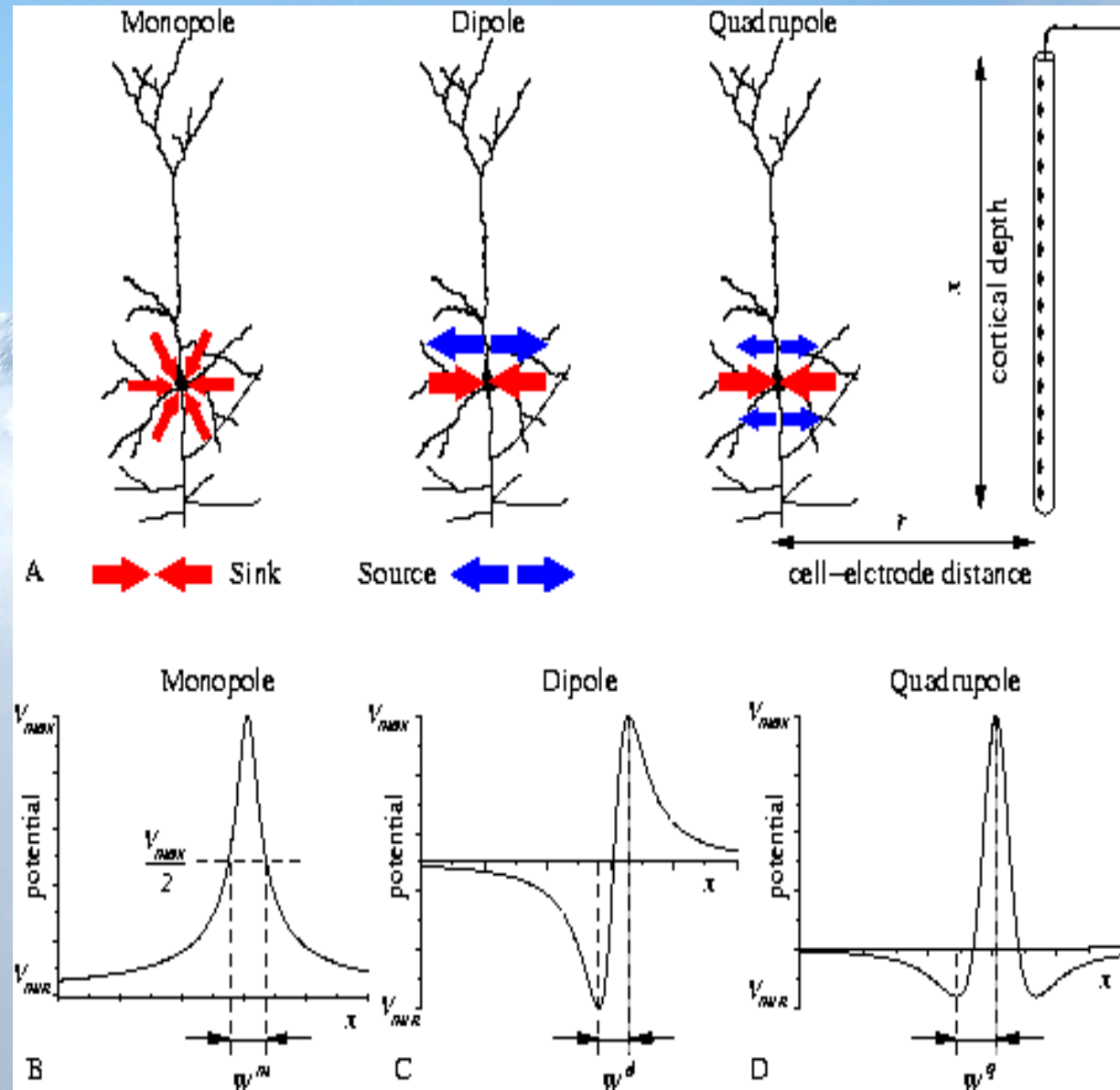
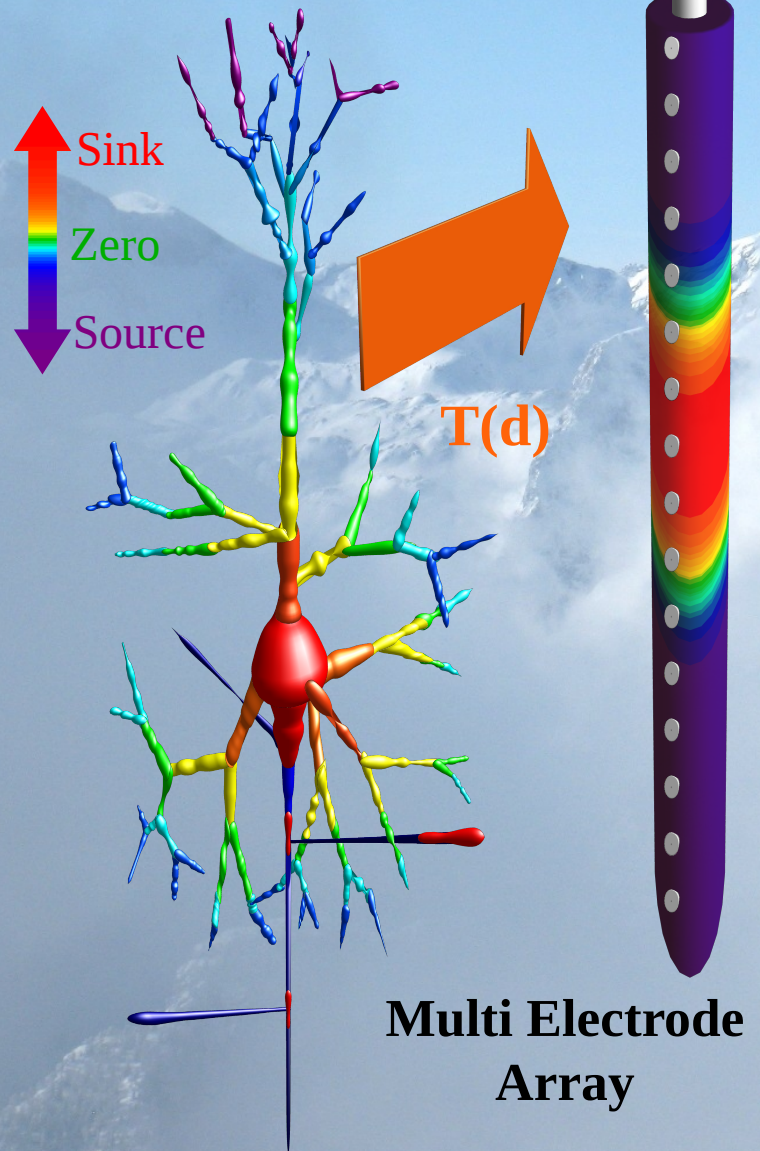
Relation between EC and IC

Simulated spatio-temporal patterns,
generated by a single synaptic pulse

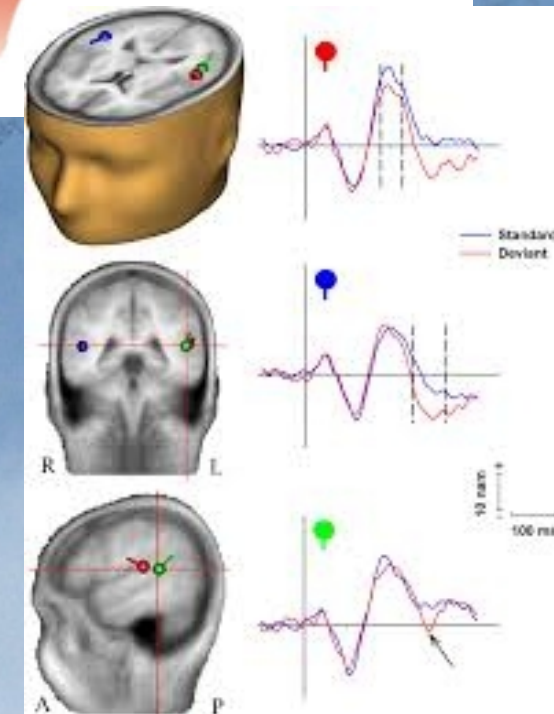
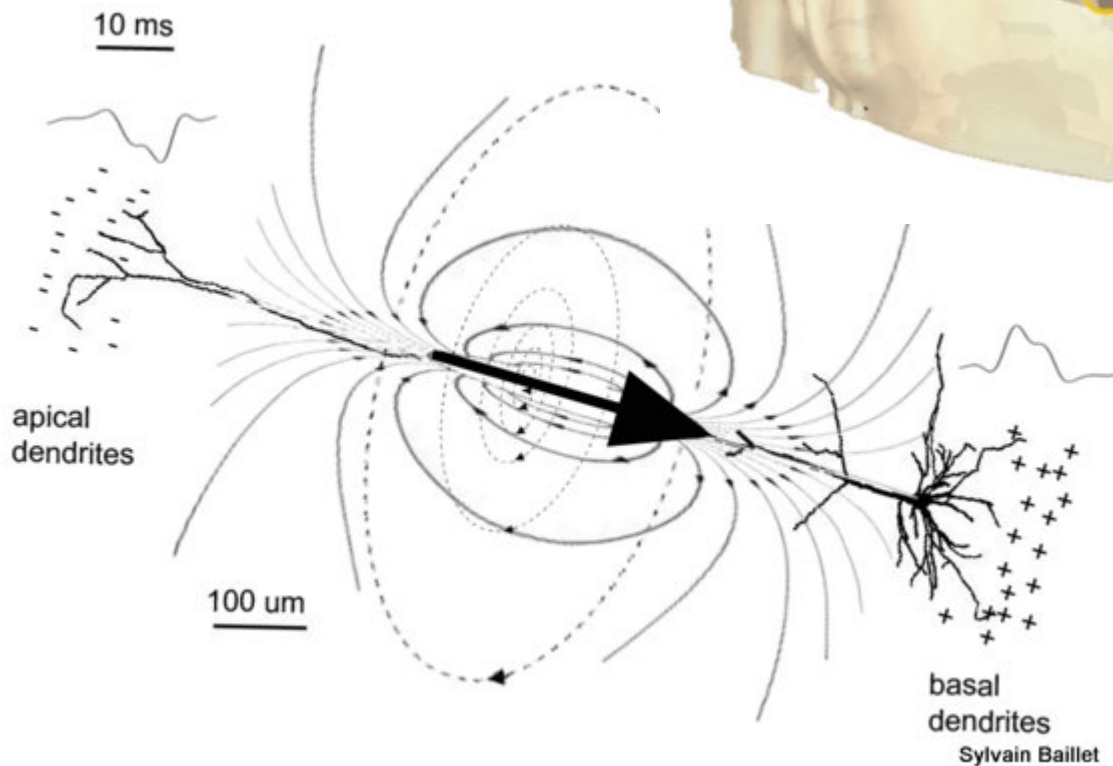
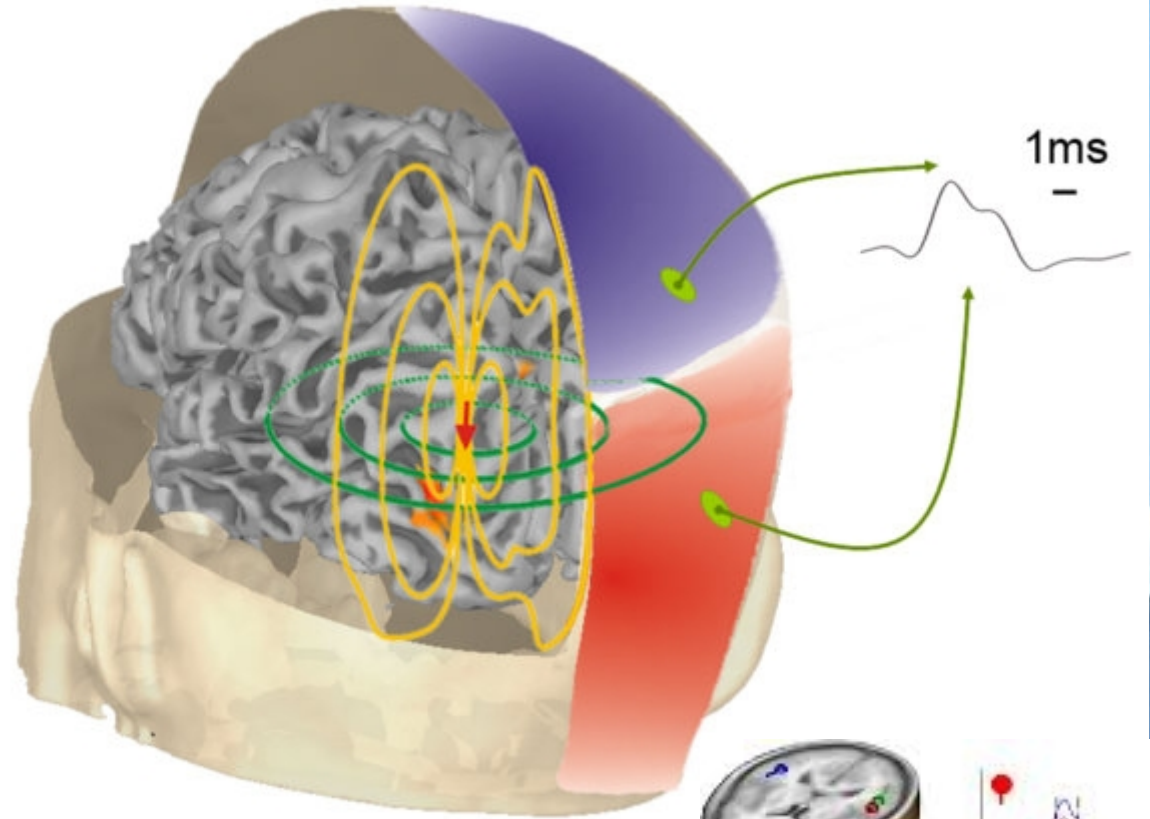


The forward problem

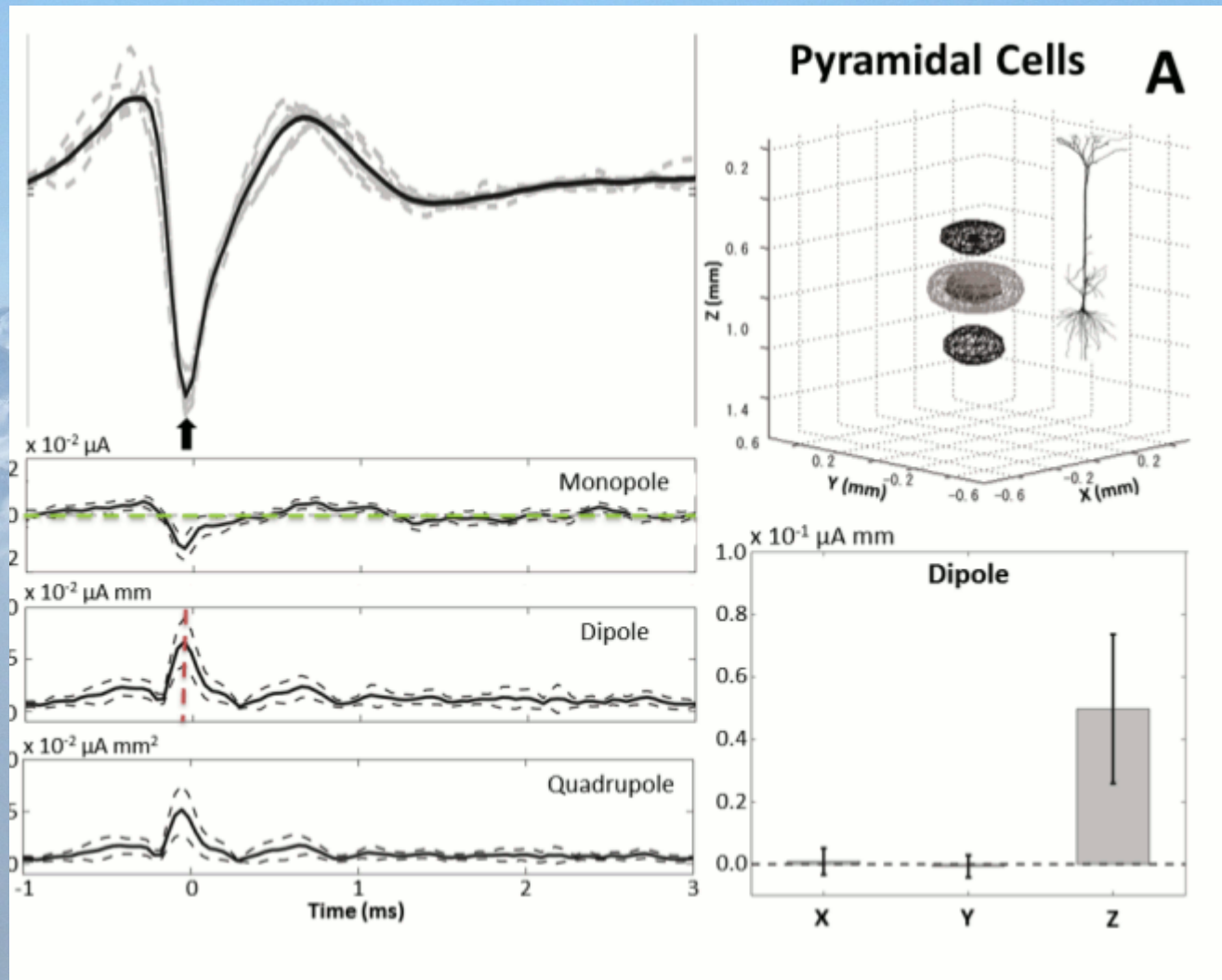
Original current source density distribution



Equivalent dipole modeling



Are neural monopole currents possible?



Riera et al.: Pitfalls in the dipolar model for the neocortical EEG sources,
Journal of Neurophysiology, 108(4):956-75, 2012

The inverse problem

Determination of transmembrane currents, flowing on the neurons, based on the extracellular potential patterns.

$$\nabla^2 V(r) = \frac{\partial^2 V(r)}{\partial x^2} + \frac{\partial^2 V(r)}{\partial y^2} + \frac{\partial^2 V(r)}{\partial z^2} = \frac{-I(r)}{\sigma_e}$$

This requires the solution of the Poisson inverse problem.

In order to perform the second derivation, the full 3D potential distribution should be known, with spatial resolution comparable to the size of the sources.

The inverse problem

The 3D potential distribution can not be measured, since a 3D electrode array would cause significant tissue damage.

Without this, **the inverse solution is not unique!**

What could be done?

Based on a priory knowledge about the source, the proper solution could be chosen among the infinitely many possible ones.

The traditional CSD method

Discretising and neglecting the derivatives in the unknown dimensions leads to the traditional CSD method:

$$I_i = \frac{-V_{i+1} + 2V_i - V_{i-1}}{dx^2 \sigma_e}$$

Implicitly we assumed, that the orthogonal derivatives are negligible, i.e. there are large homogeneous laminar sources.

The traditional CSD method

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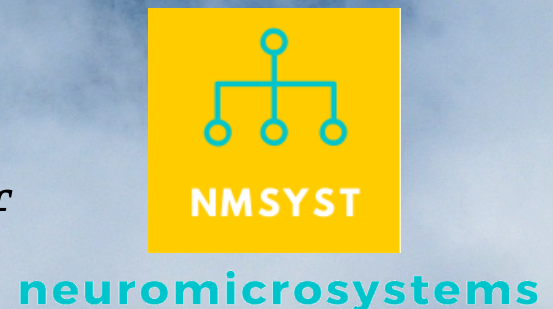
Micro-electro imaging: Determination of cortical and synaptic layers and synaptic dynamics based on extracellular multi-electrode potential measurements

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Sciences*

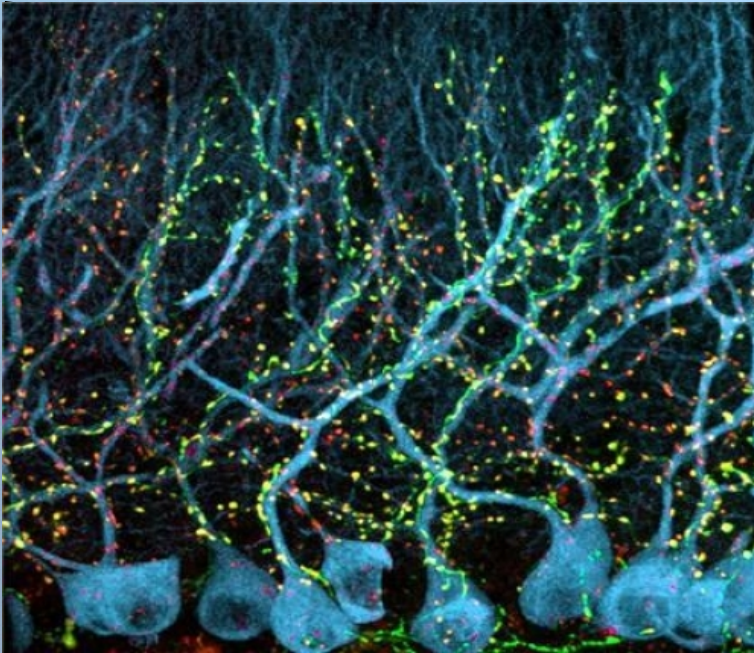
Department of Theory



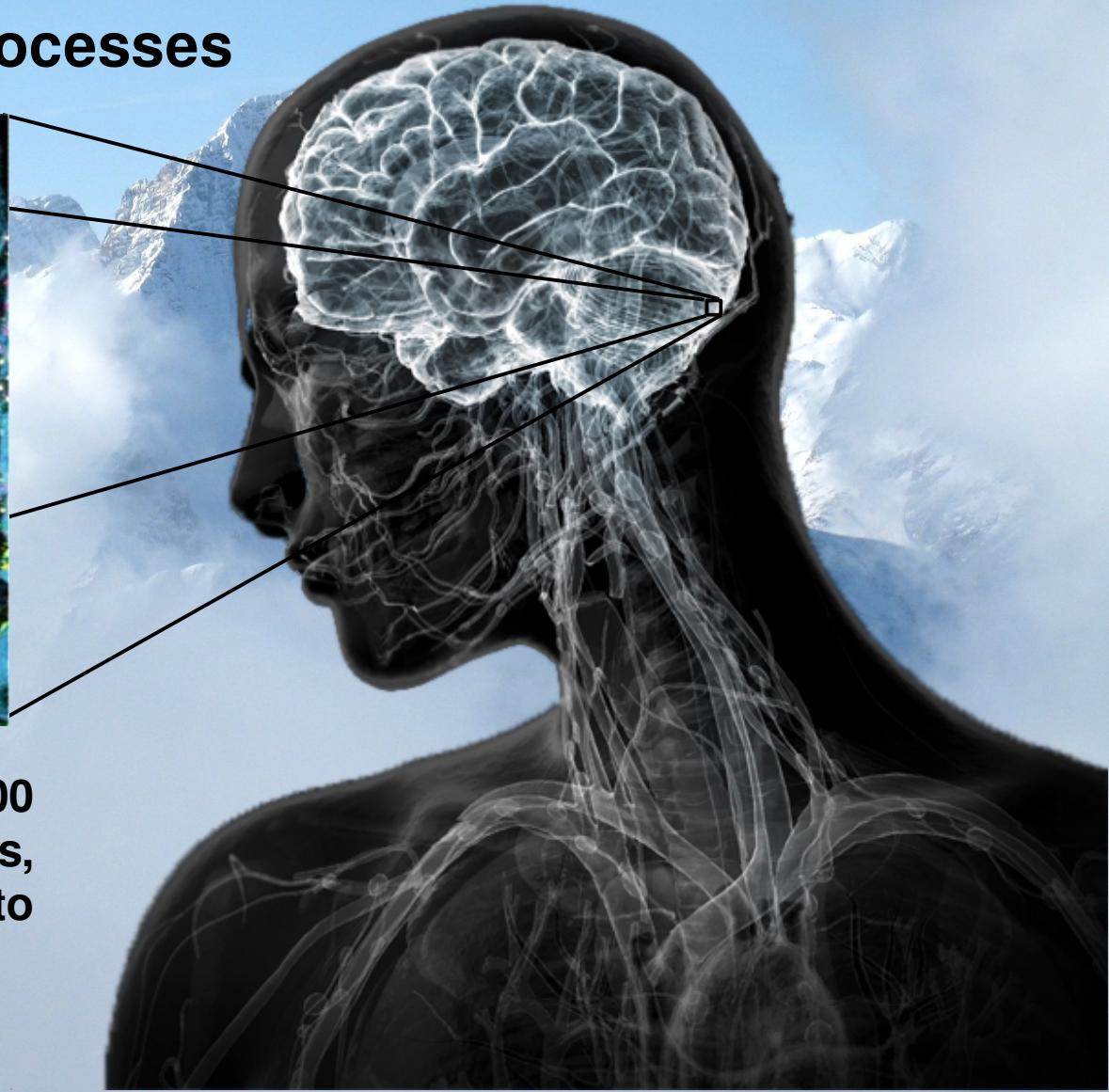
Micro-electro imaging

The gray mater of the brain

Dense tissue of the neural processes



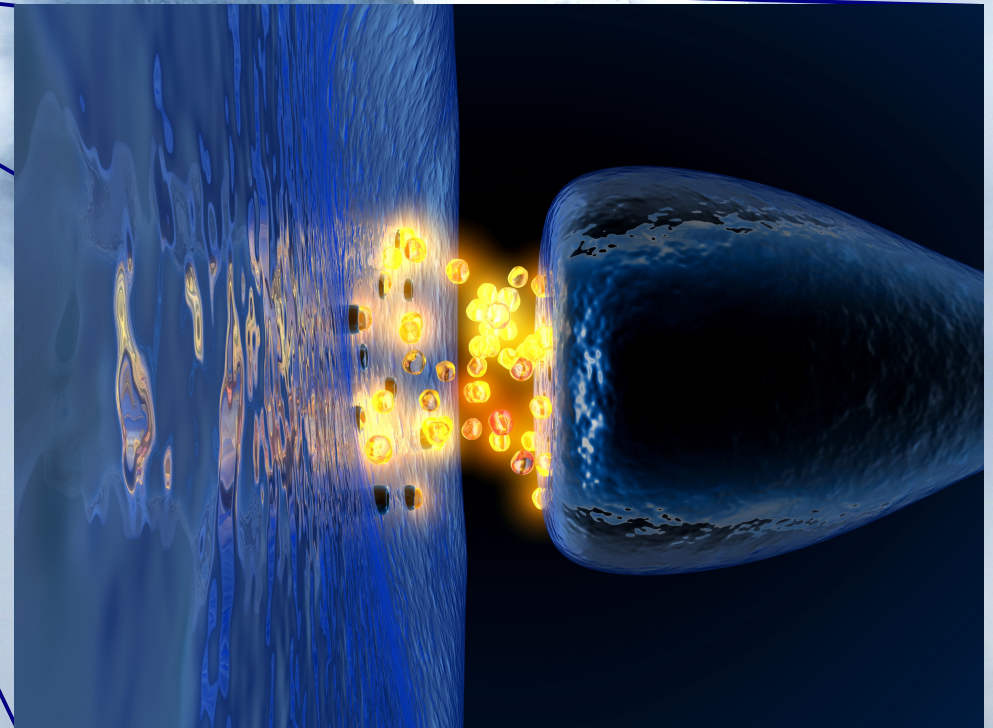
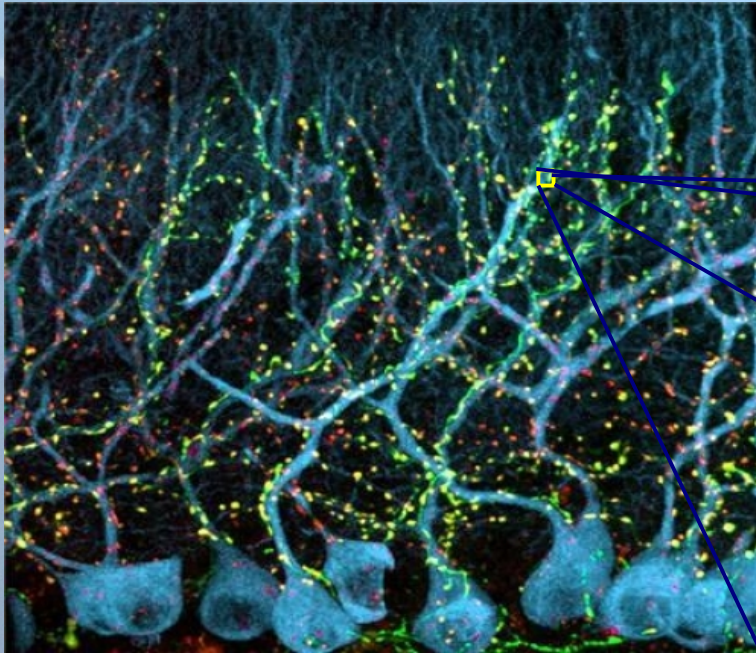
An average neuron receives 15000 input synapses from other neurons, but in some cases it grows up to 500000.



Micro-electro imaging

Synapse: communications between neurons

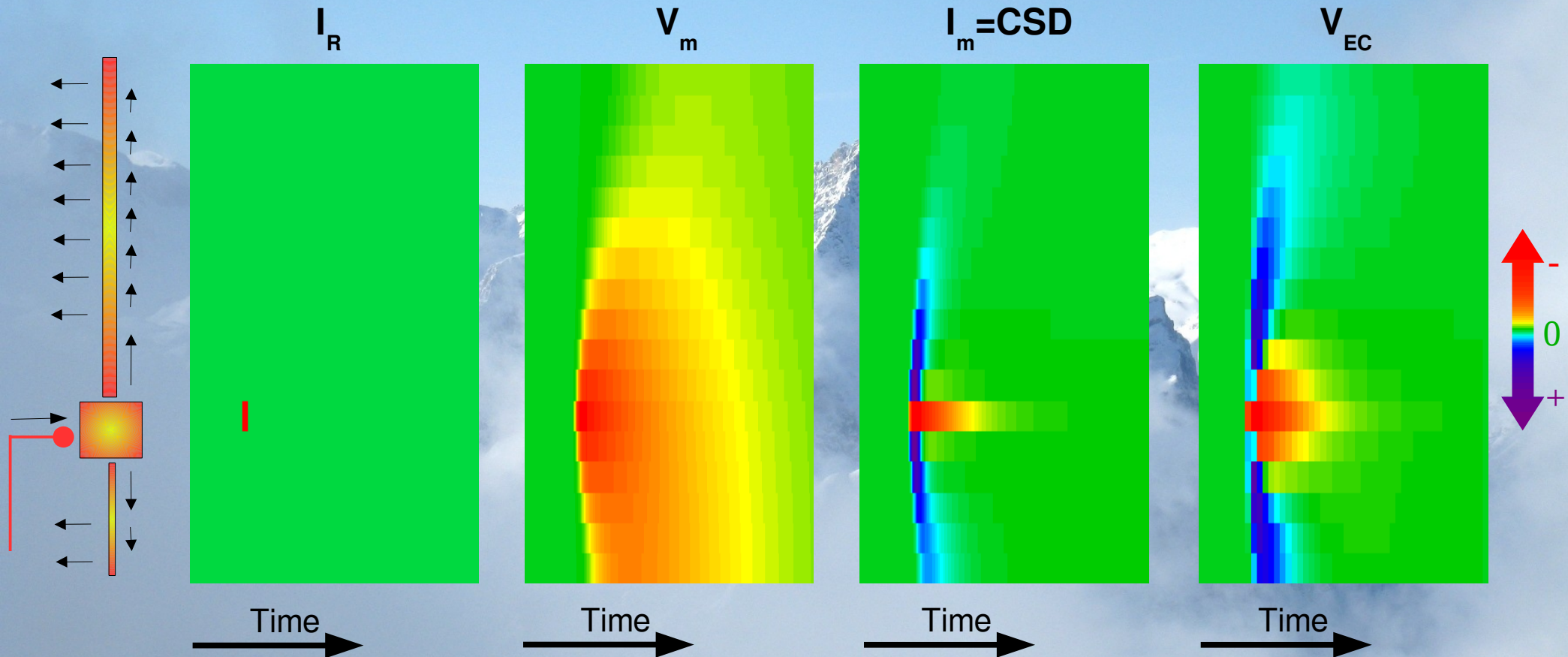
Opening of the ion channels due to binding of the neurotransmitter molecules initiates a wave of currents on the membrane.



An average neuron receives 15000 input synapses from other neurons, but in some cases it grows up to 500000.

Micro-electro imaging

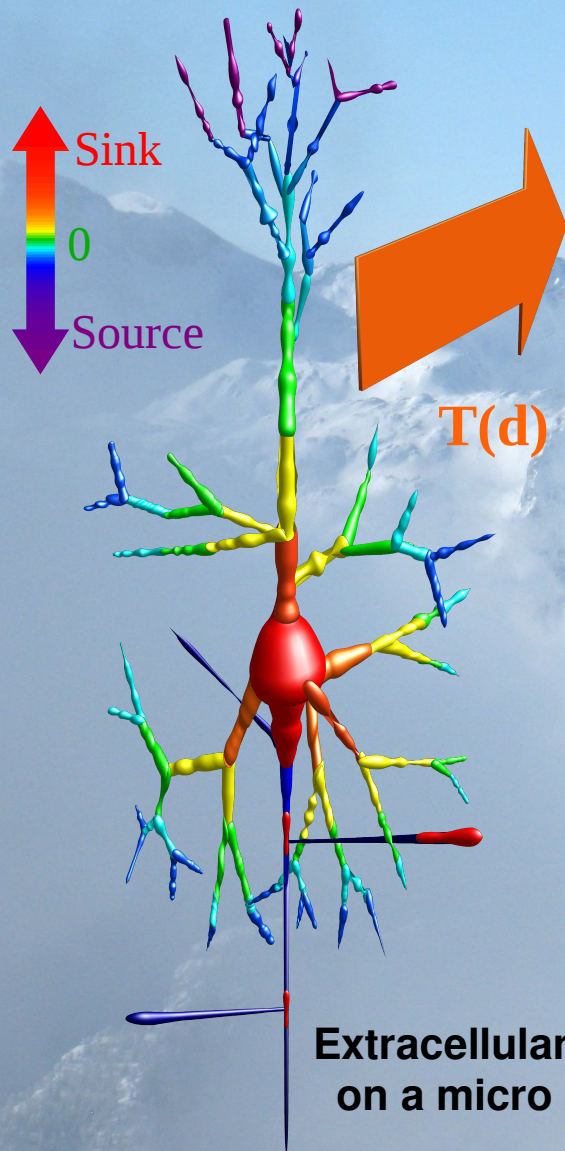
A single simulated synaptic pulse



Even a single current pulse into the simulated neuron generates quite complex spatio-temporal pattern of extracellular potential

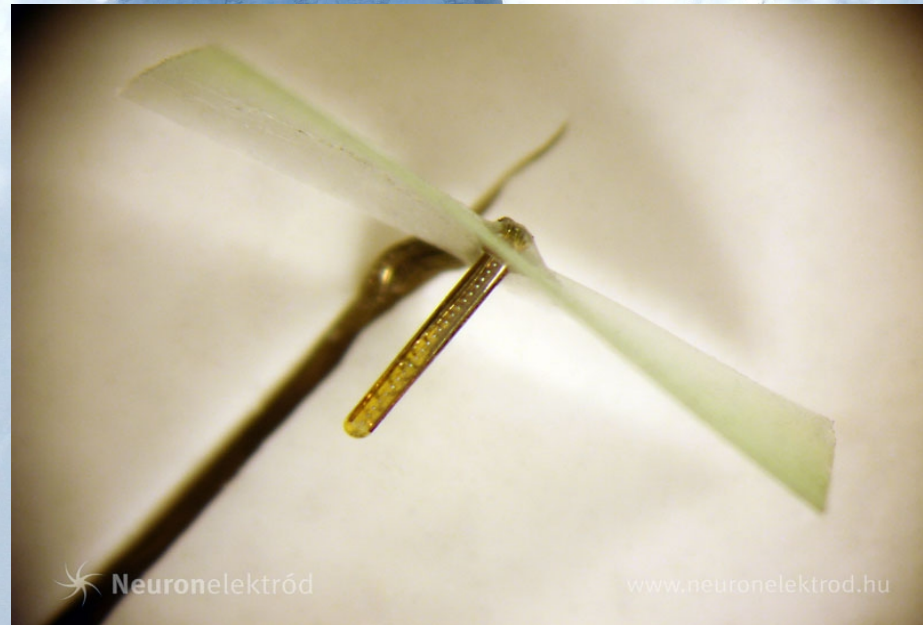
Micro-electro imaging

Current source
density distribution
on the cell



Micro electrode arrays

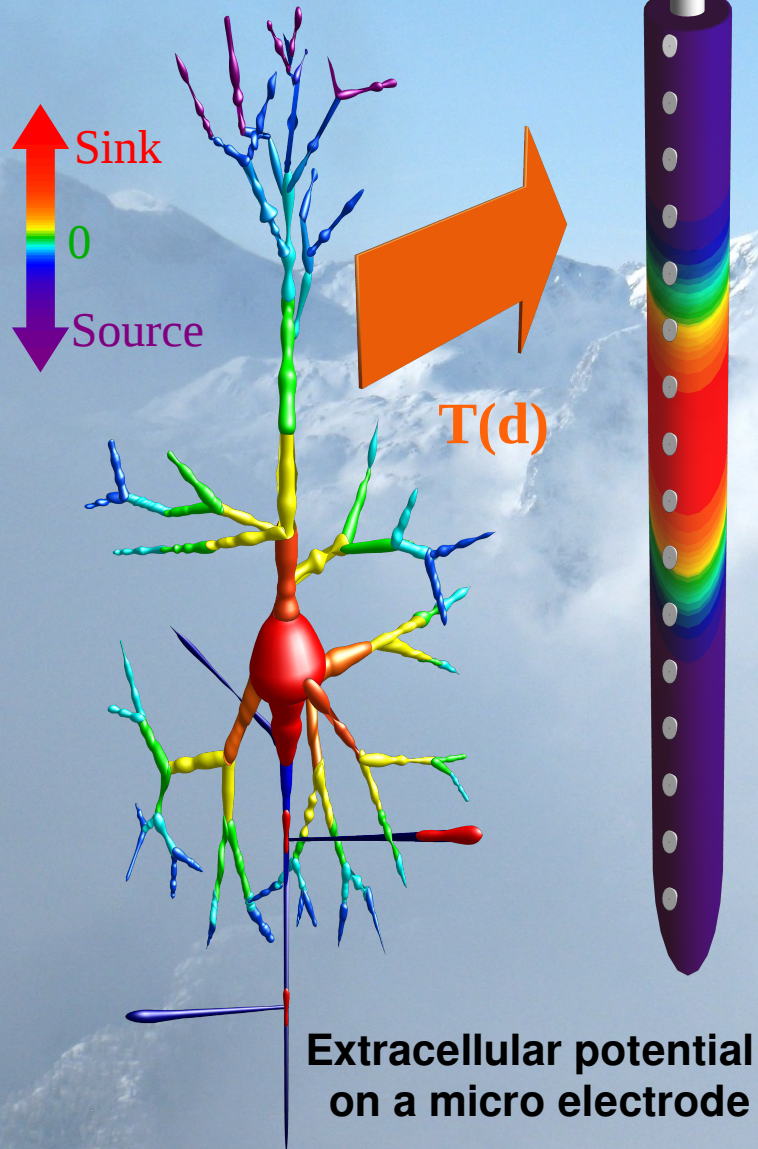
By chronically implanted micro electrode arrays, the EC potential of the neurons can be monitored during awake behaving animals.



Extracellular potential pattern
on a micro electrode array

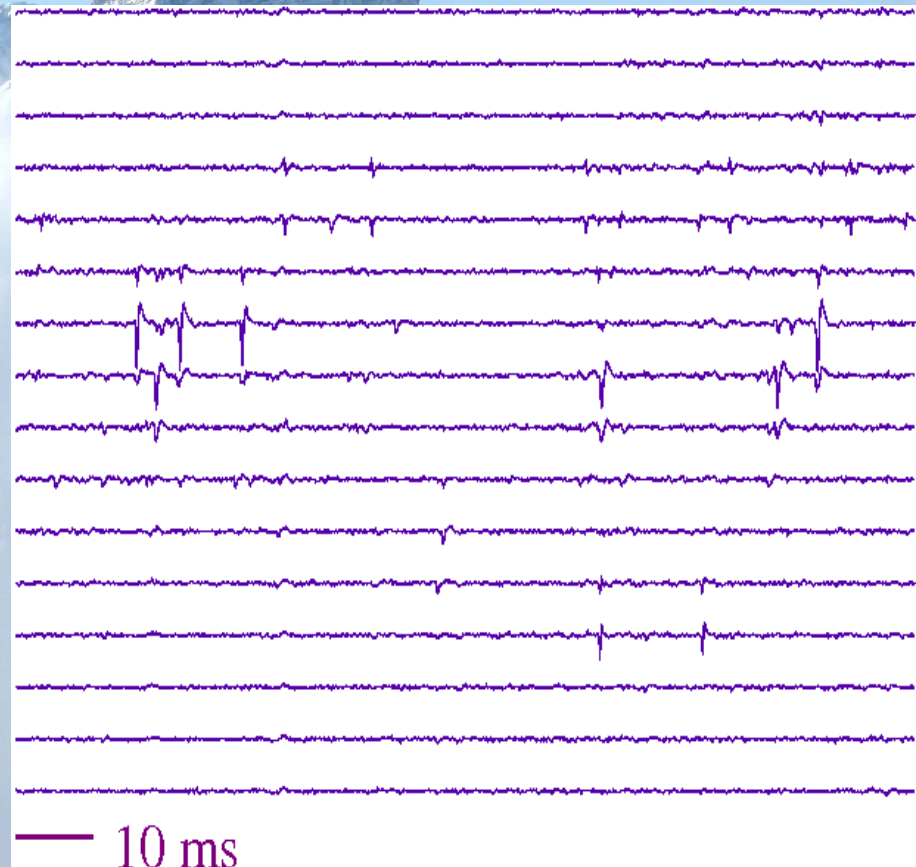
Micro-electro imaging

Current source density distribution on the cell



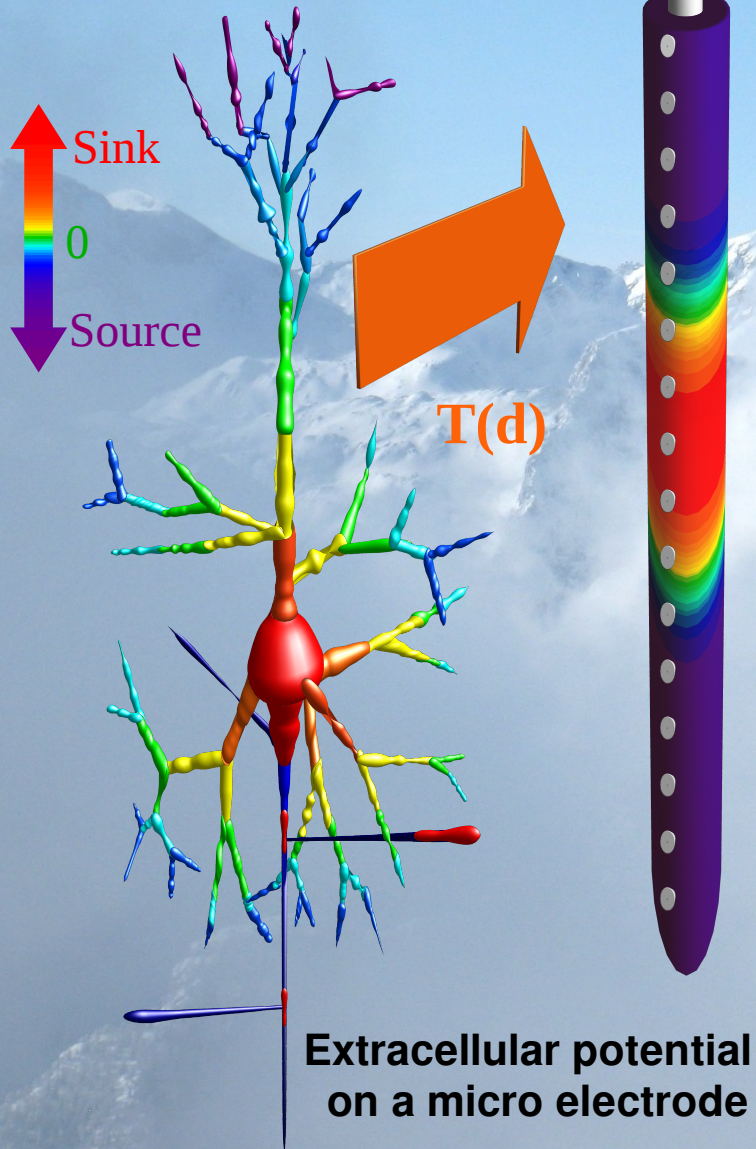
The output of the neurons

The EC potentials of the individual neurons are easily recognizable on the high pass filtered recordings, representing the output of the neurons.



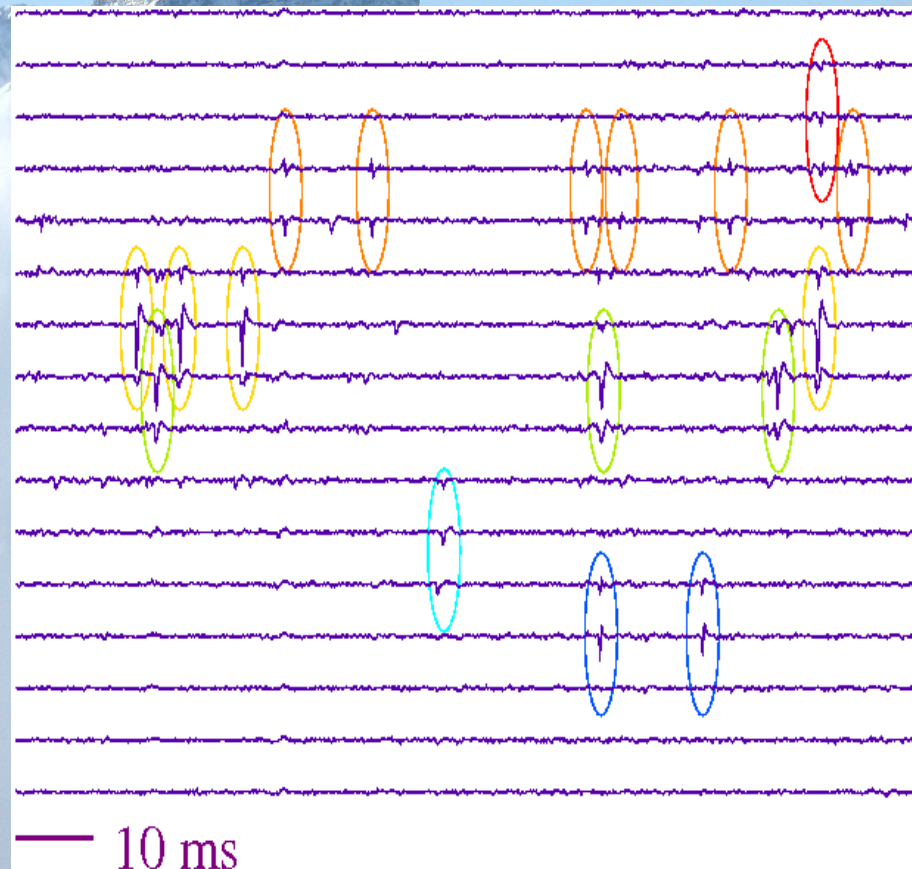
Micro-electro imaging

Current source
density distribution
on the cell



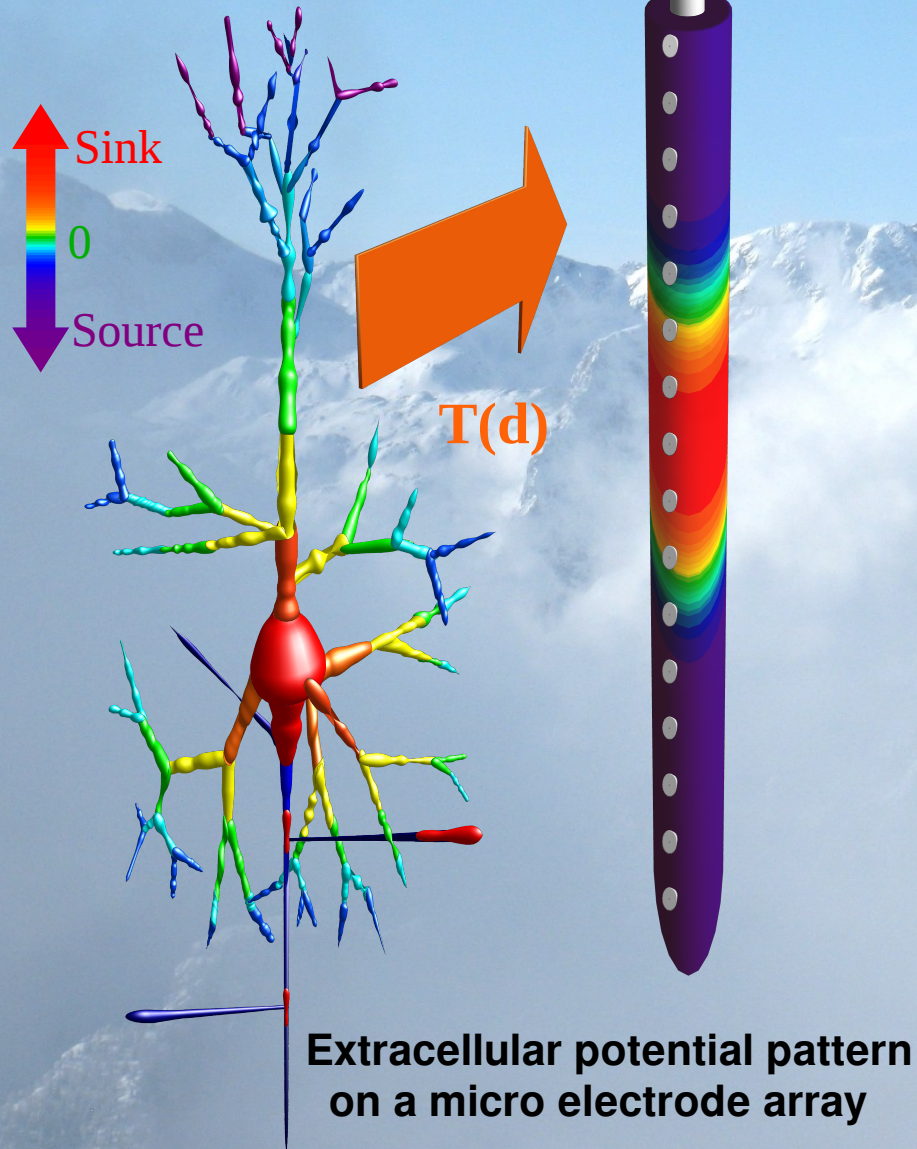
The output of the neurons

The spikes of the individual neurons can be distinguished based on the different signal form and relative amplitudes.



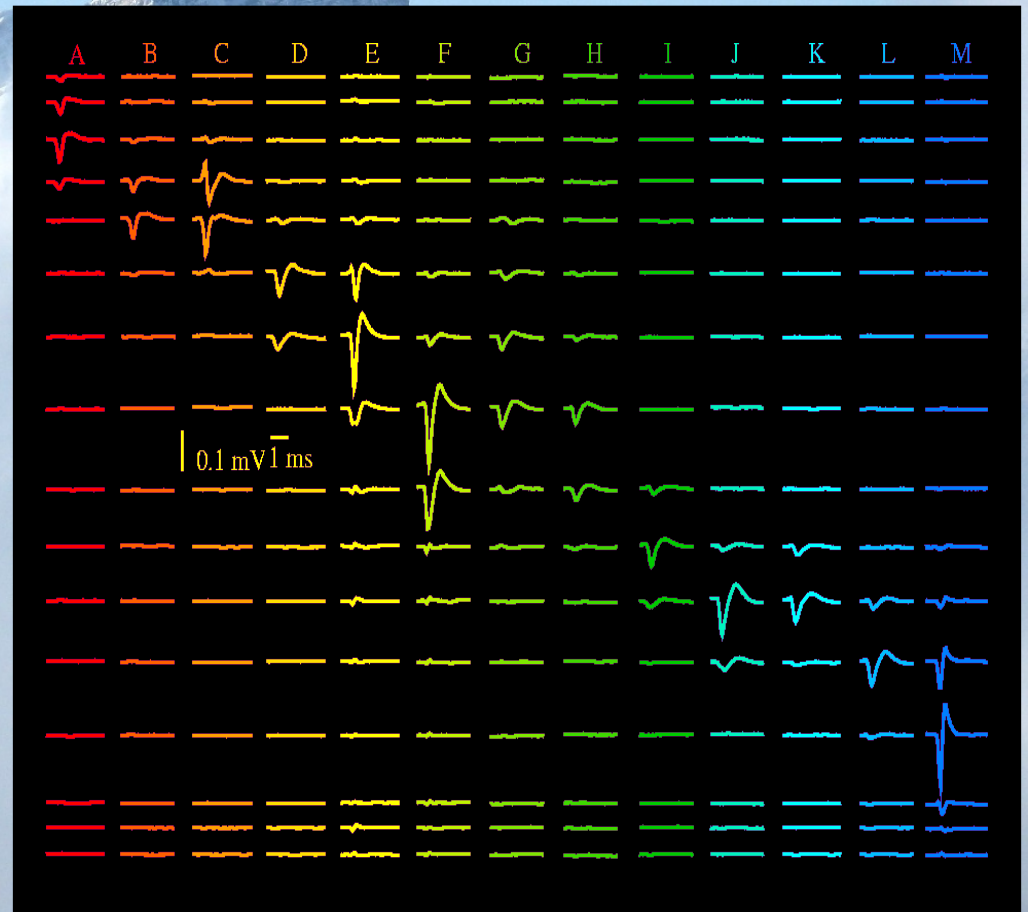
Micro-electro imaging

Current source density distribution on the cell



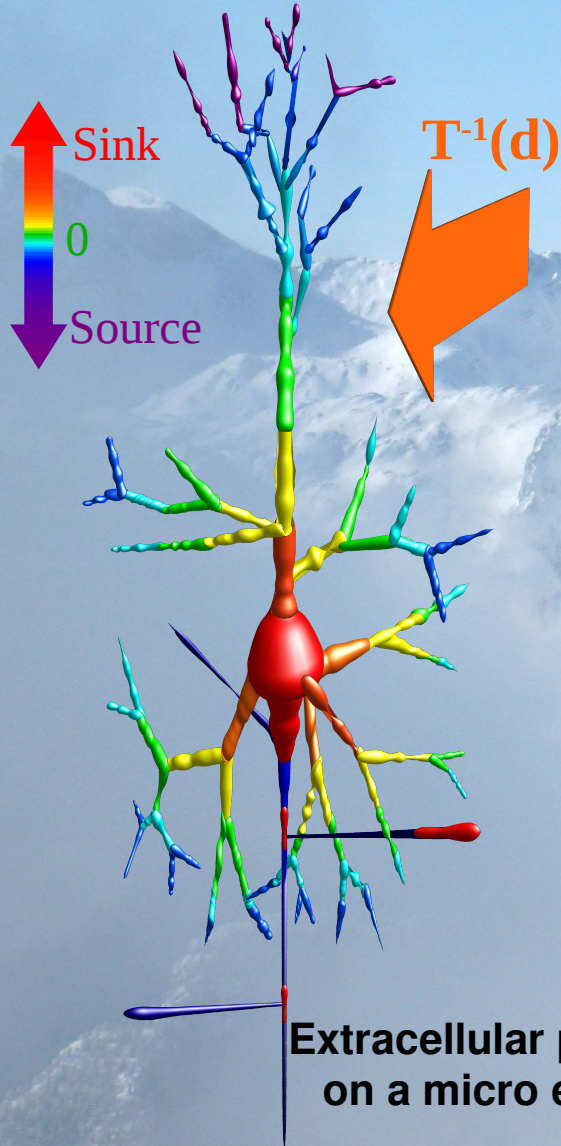
The output of the neurons

Each neuron generates a specific spatio temporal potential pattern (marked with different colors)



Micro-electro imaging

Current source
density distribution
on the cell



The problem

The dendritic integration is relatively well understood.

It is possible to measure and identify the output of the individual neurons.

BUT

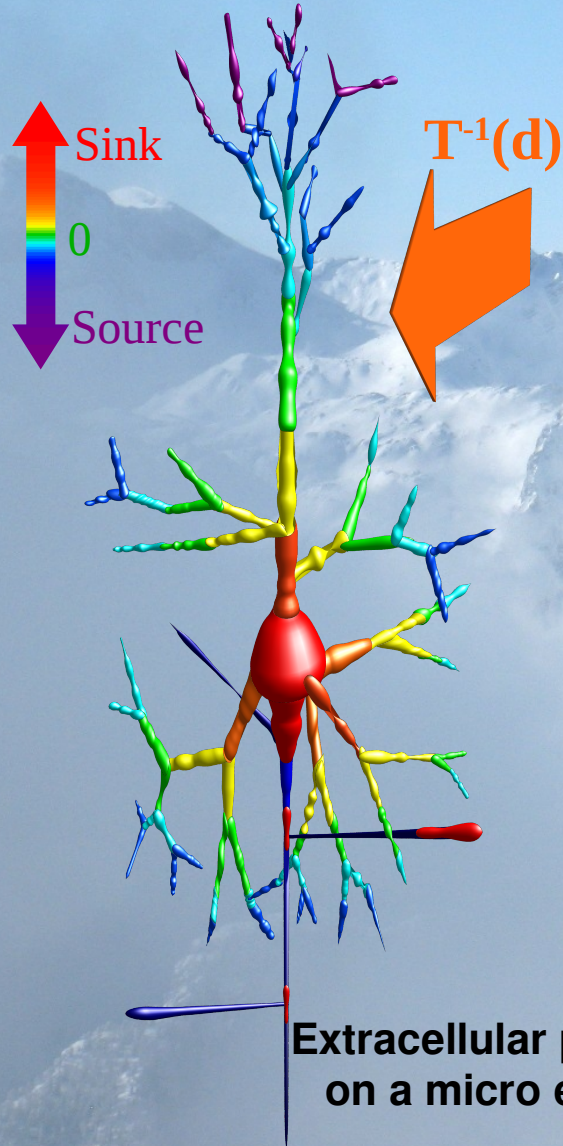
We have no clue of that what spatio temporal synaptic current pattern emerges on the dendrites from the integration of enormous number synaptic input impulses.

There is no proper measuring technique!

Without knowing the inputs, understanding the elementary computation performed by individual synapses is hopeless.

Micro-electro imaging

Current source
density distribution
on the cell



The idea

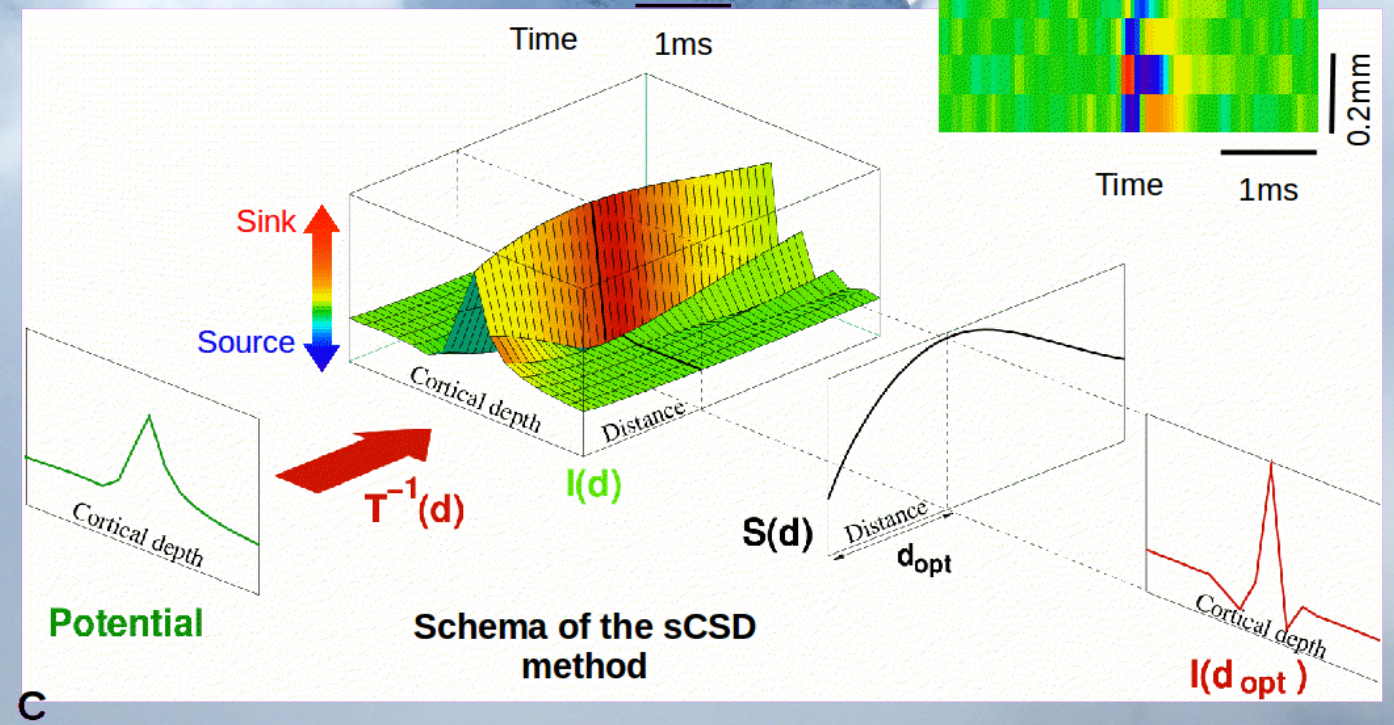
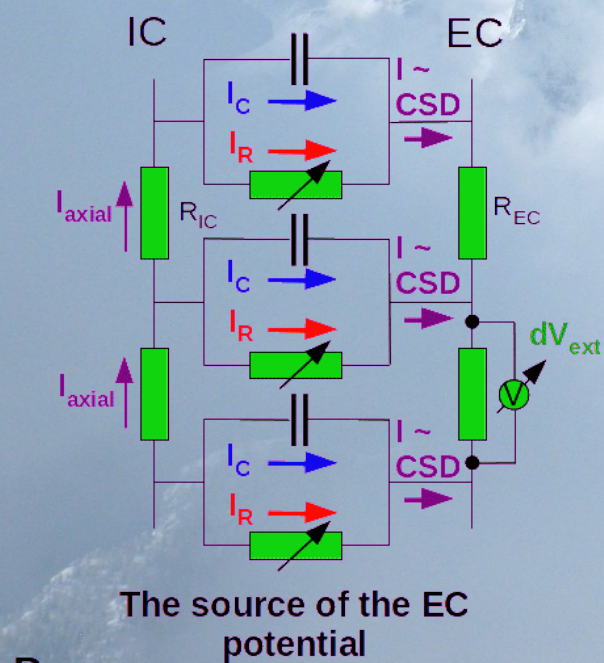
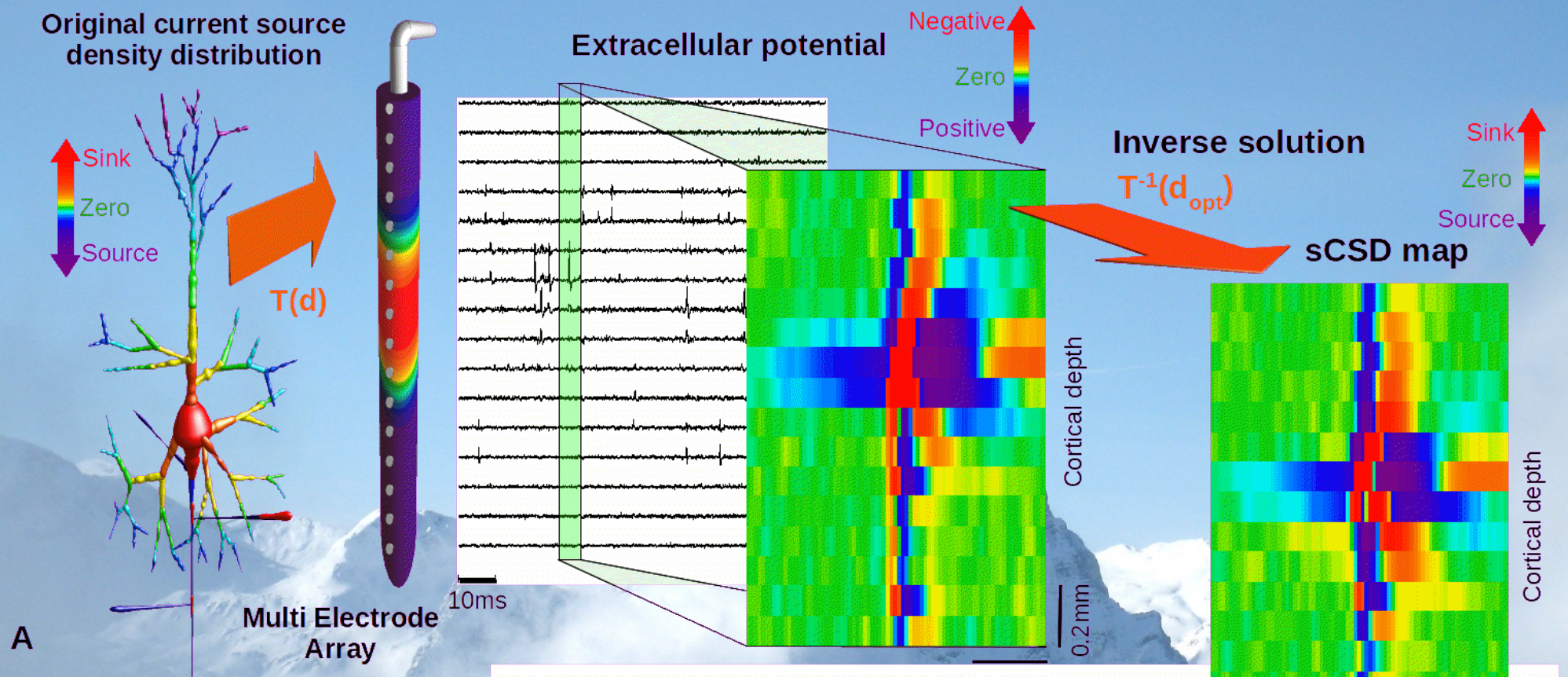
Source reconstruction by inverse methods:
Inverse solution of the Poisson-equation
under special constraints which incorporate
our a priori knowledge to the solution and
makes it unique.

'Autofocus' algorithm for position estimation
of the neurons

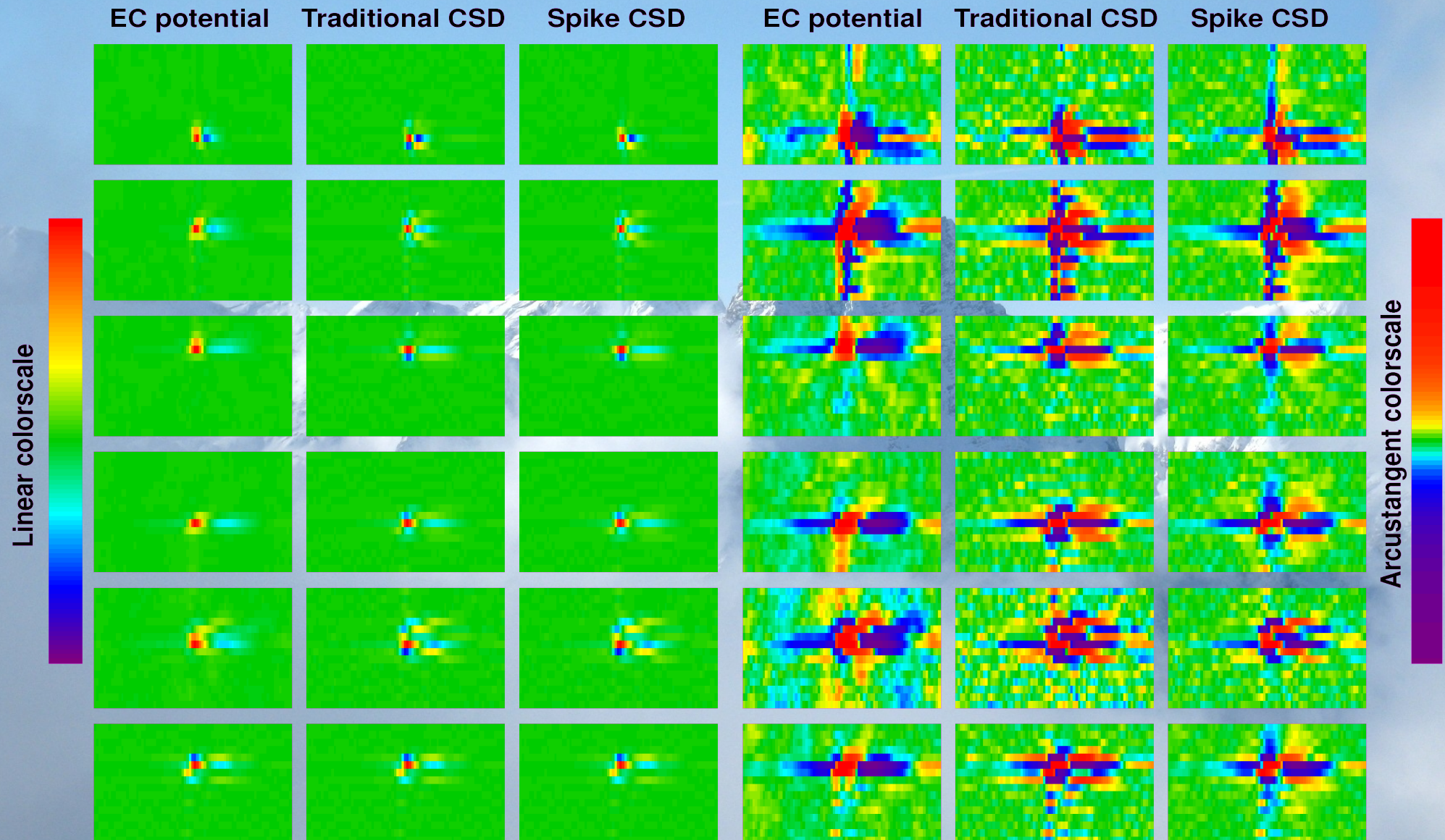
Analogous to the ultra resolution microscopy,
where objects can be resolved beyond the
Nyquist limit



Extracellular potential pattern
on a micro electrode array



What is essential, is invisible to the eye



1-5% relative amplitudes are typically significant

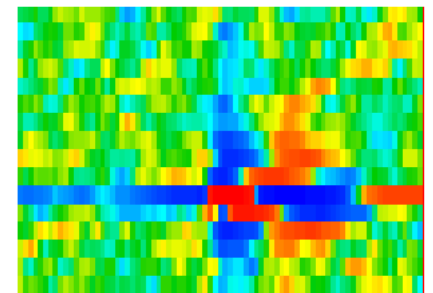
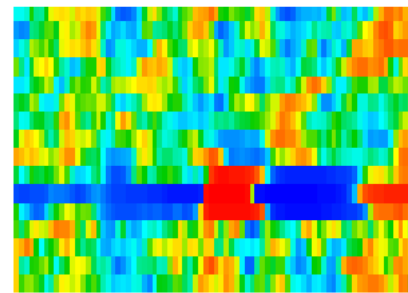
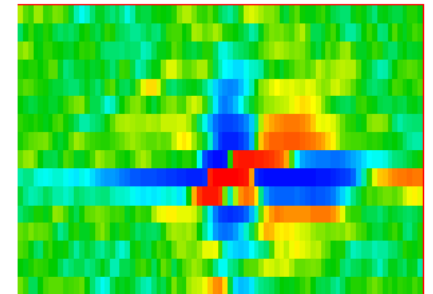
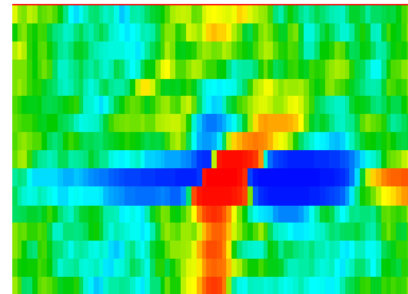
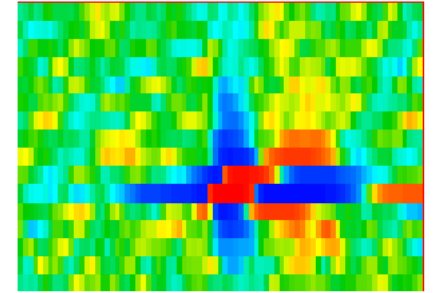
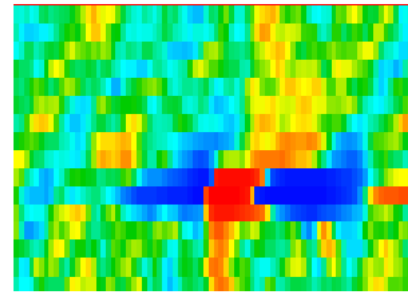
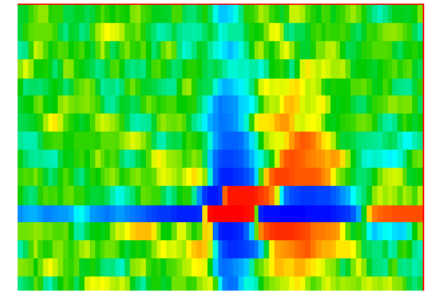
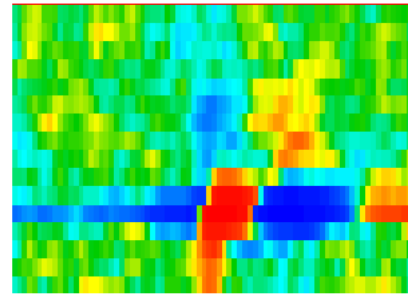
Spatio- temporal dynamics of the action potentials

New fine details revealed by
the application of the new
SCSD method

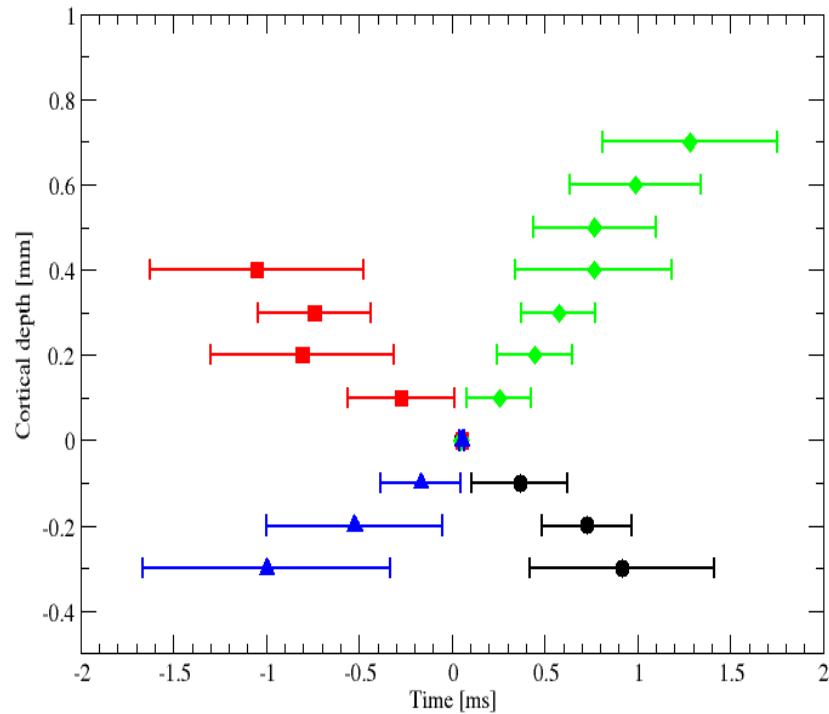
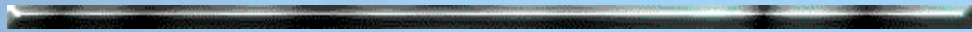
Besides apical, basal back-
propagation became
observable.

Potential

sCSD

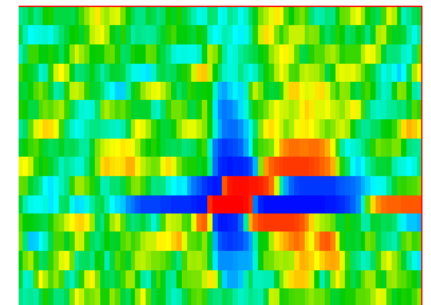
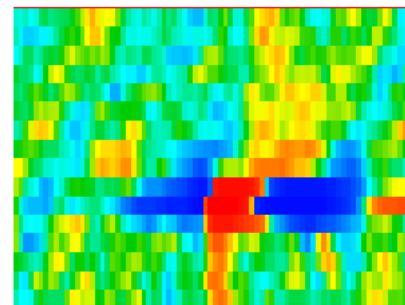
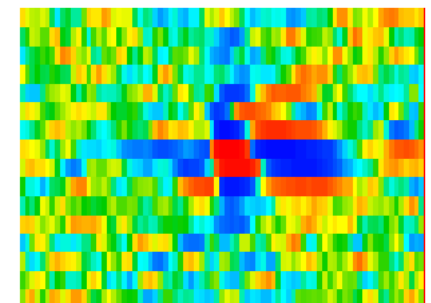
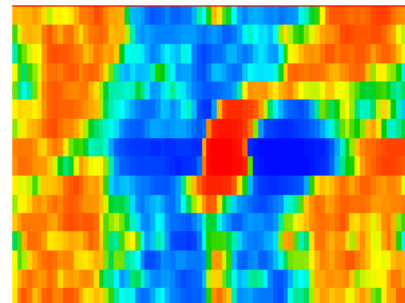
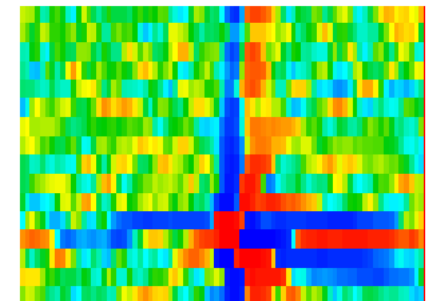
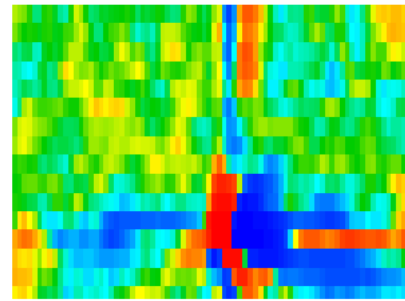
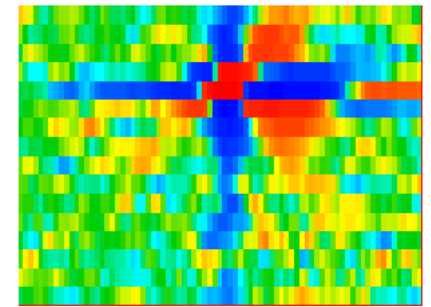
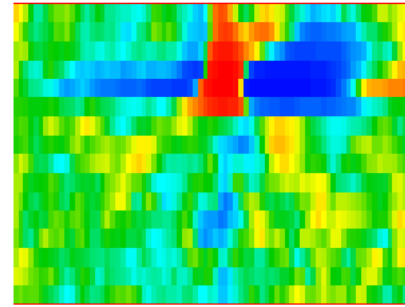


Some signs of forward propagation appears

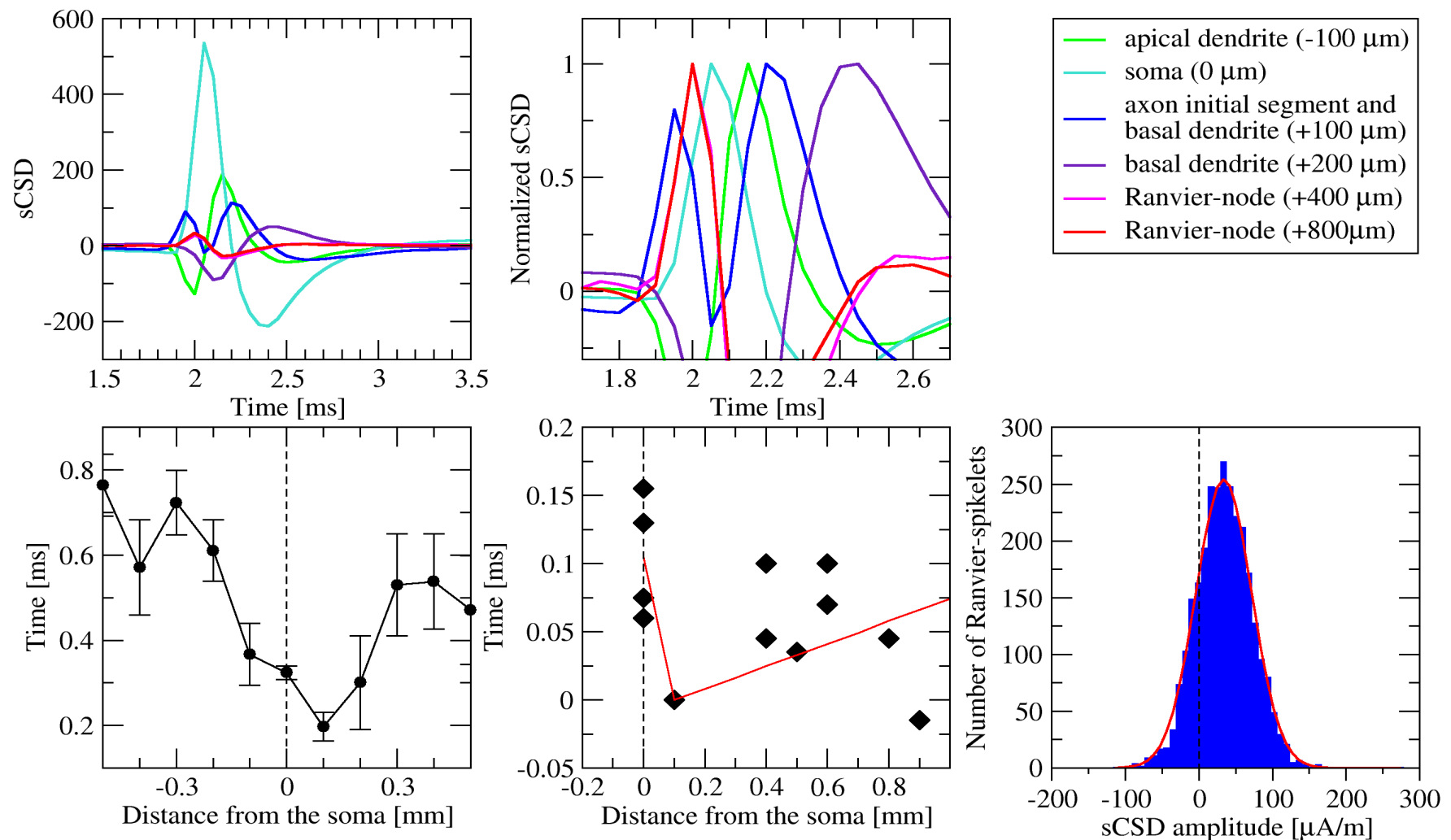


Potential

sCSD



Initiation and spreading of the action potential

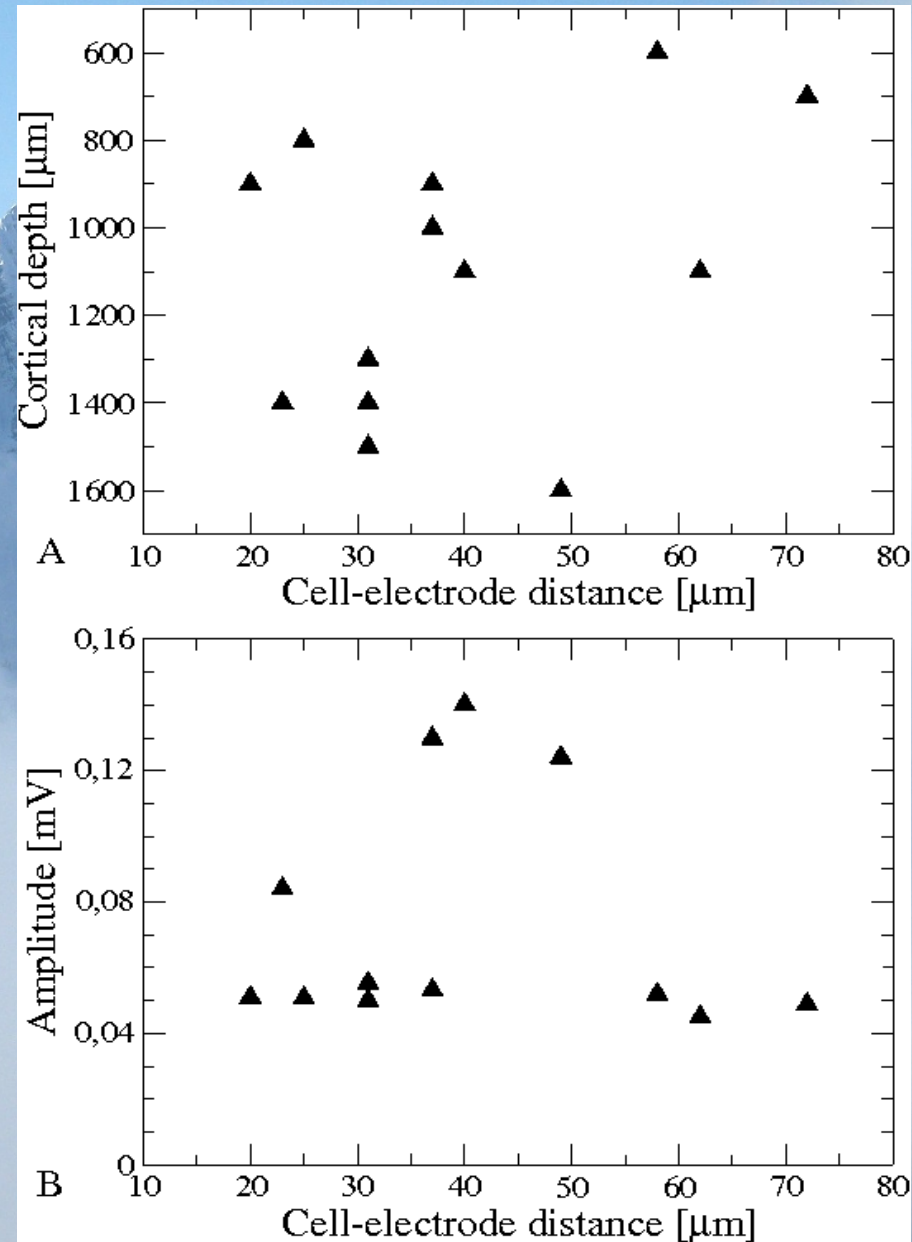


An opportunity for indirect verification

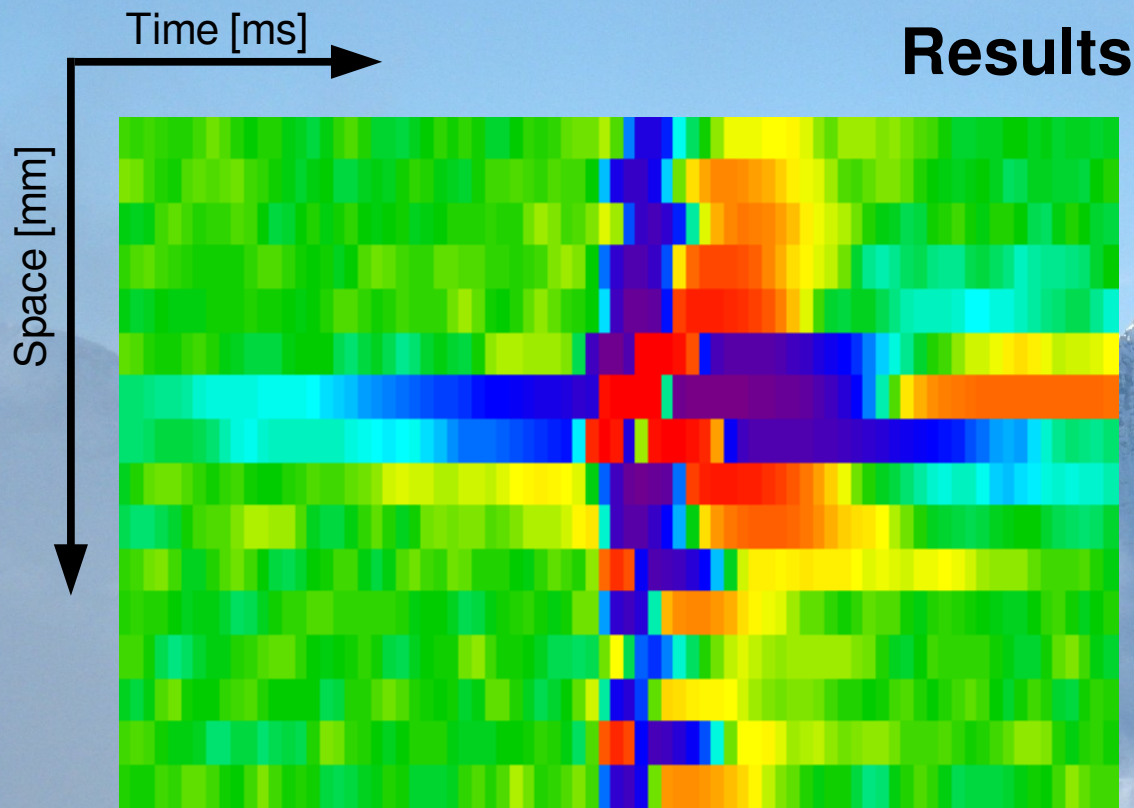
Henze et al. J. Neurophysiol. 2000:
Action potentials can be measured
from 200 μm distance, but reaches the
60 μV amplitude only in 60 μm
vicinity, which is required for the
successful spike sorting.

We assumed a priori, that $d < 200 \mu\text{m}$

The result: $\max(d) = 72 \mu\text{m}$



Micro-electro imaging

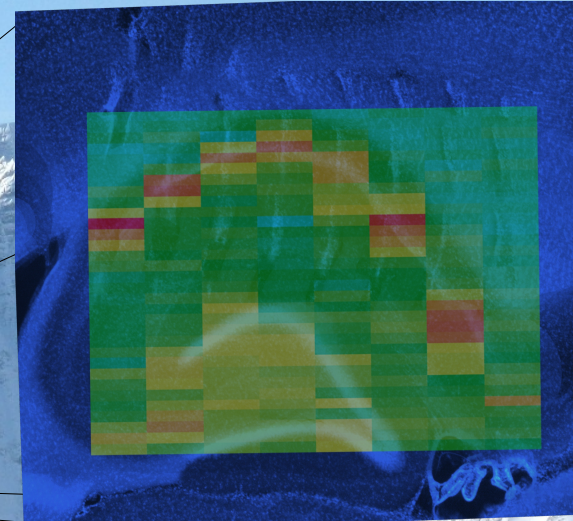
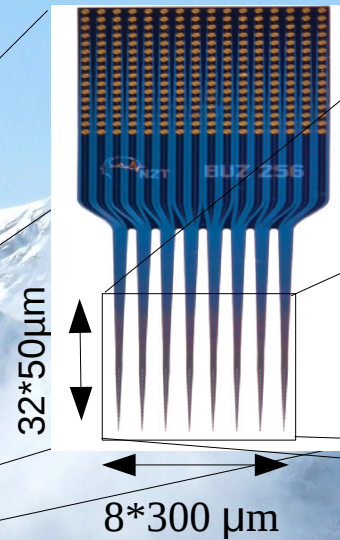


We showed, how the action potential is generated and spread back to the apical and basal dendrites and propagates along the myelinated axon.

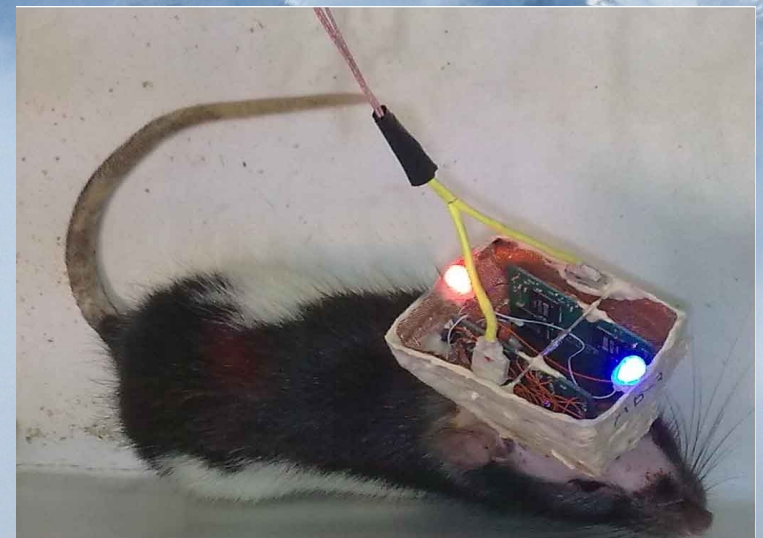


Micro-electro imaging

2 dimensional, 256 channel electrode system

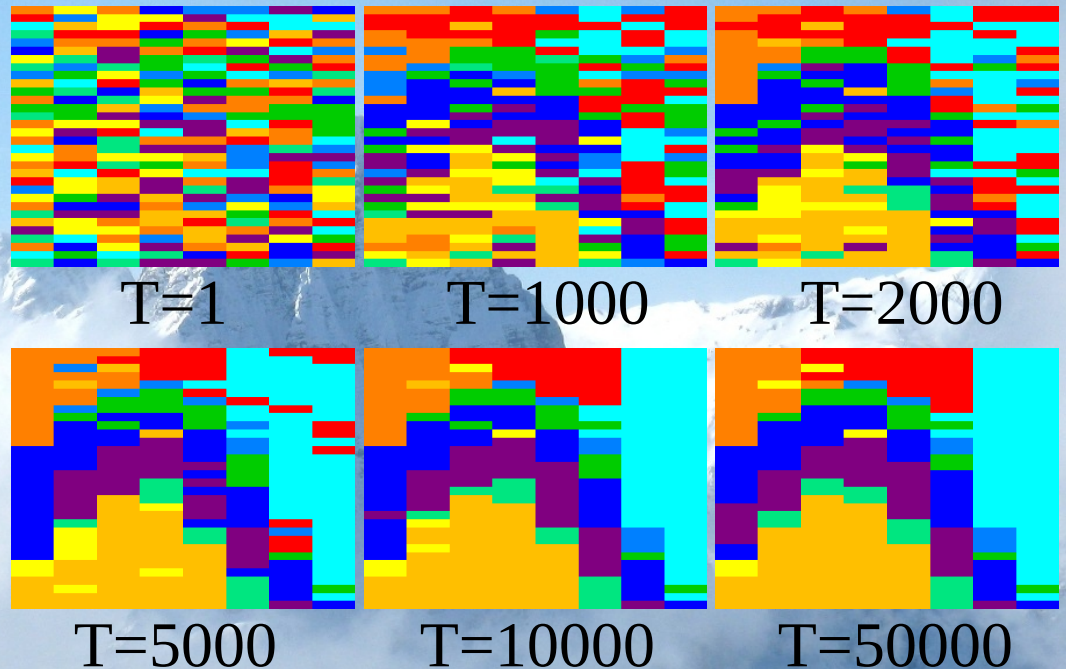
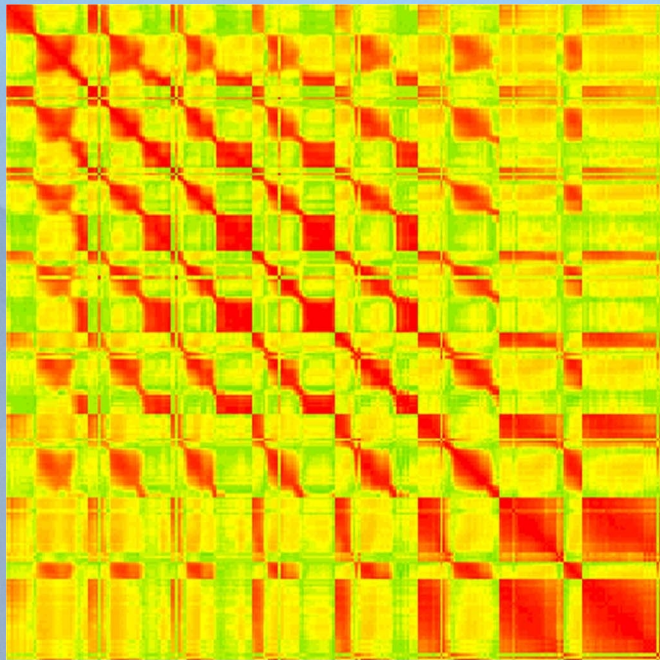


Made possible parallel monitoring of the many subareas of the hippocampus and cc. 100 sorted and identified neurons.



Micro-electro imaging

Micro-electro anatomy



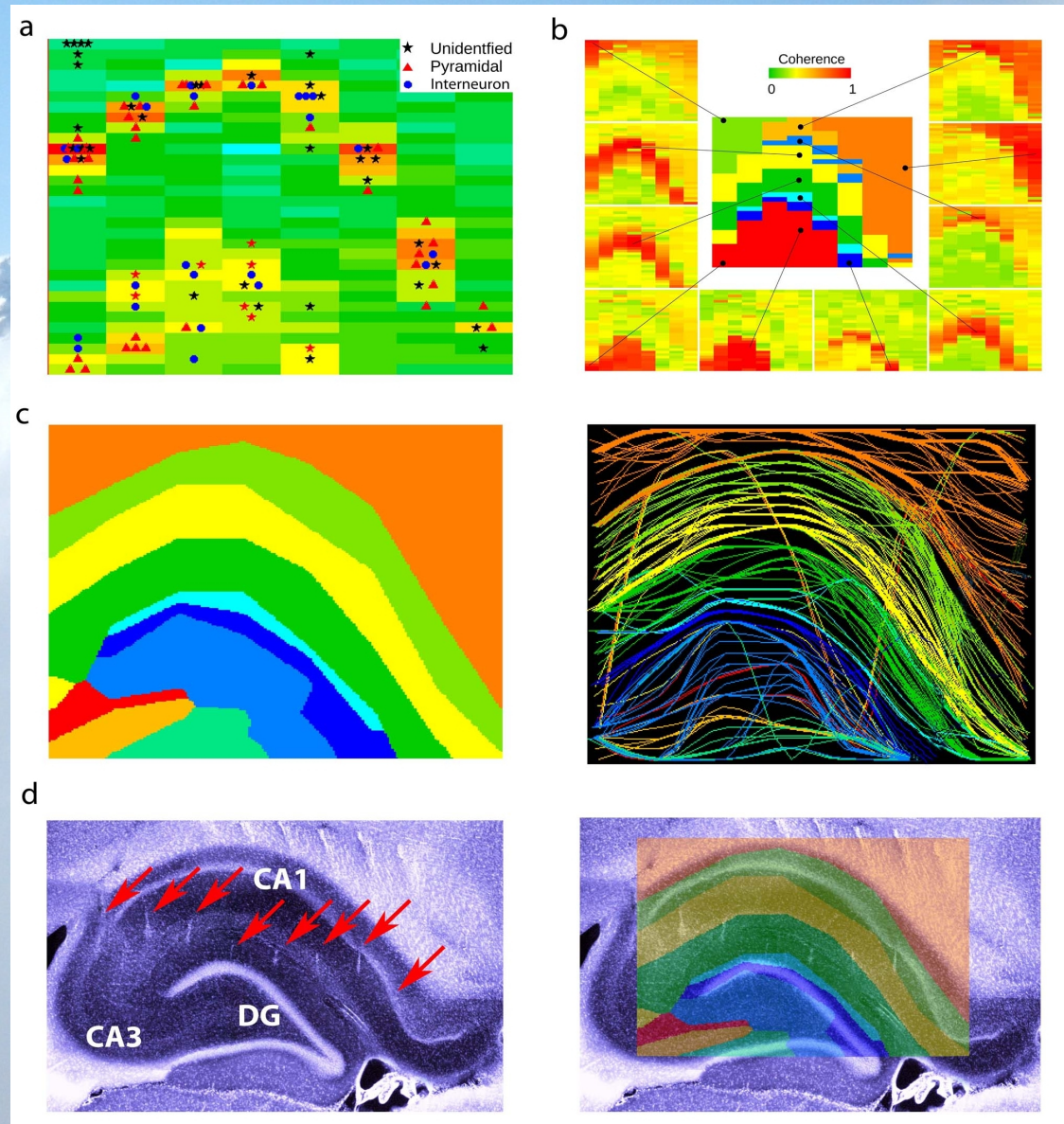
Layer structure of the hippocampus are revealed under the assumption, that the channels in the same layer receive similar synaptic inputs, but with different temporal delays. Thus coherence and the coherence based clustering could reveal the anatomical layers.

Micro-electro imaging

Micro-electro anatomy

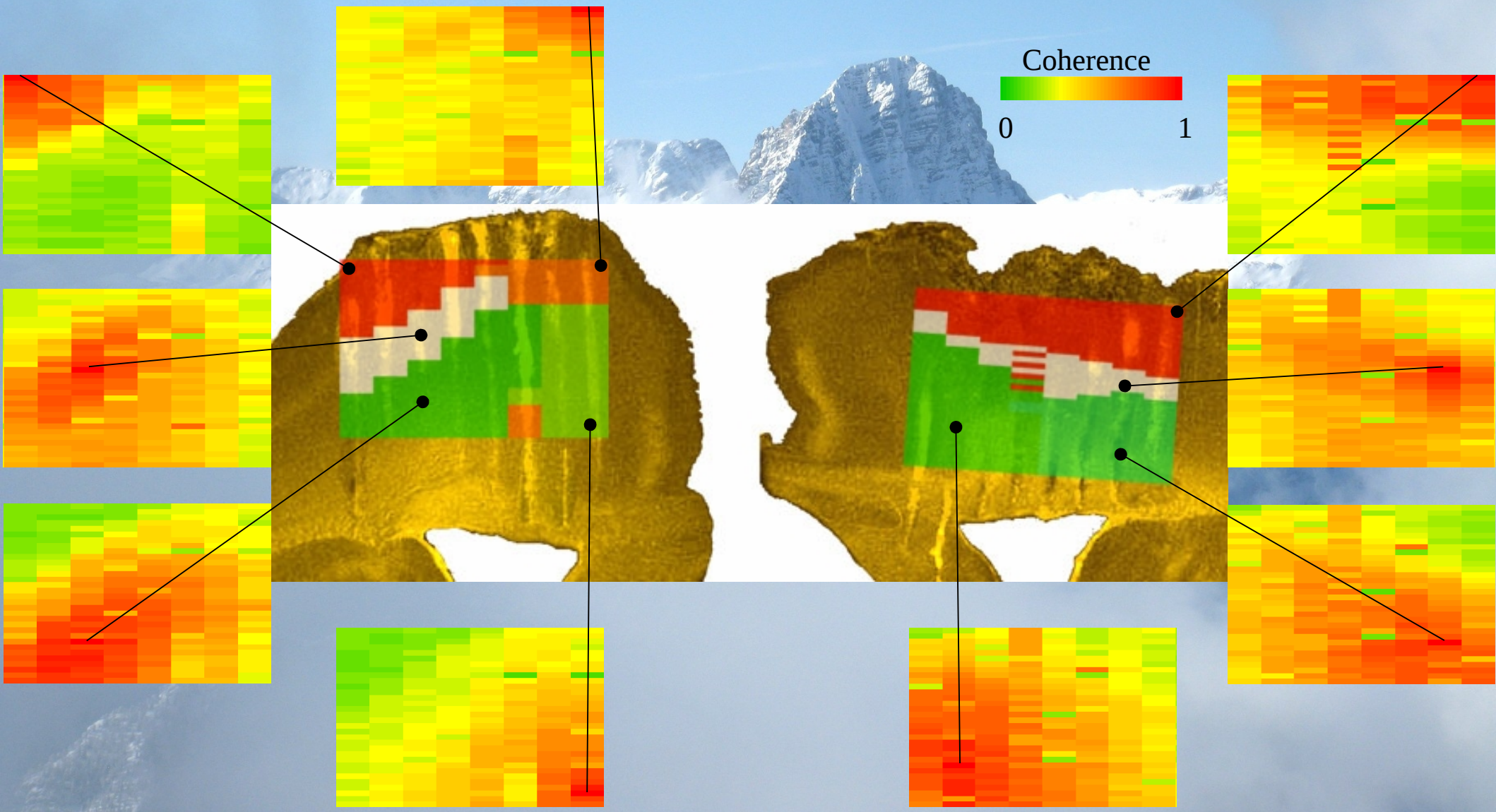
The high frequency power map show the somatic layers, which corresponds to the positions of the sorted individual neurons. The fusion of this high frequency power map with the result of the coherence clustering resulted a detailed layering map of the hippocampus. This electro-anatomical map corresponded well to the tissue histology.

Berényi et al. J Neurophysiology
2014



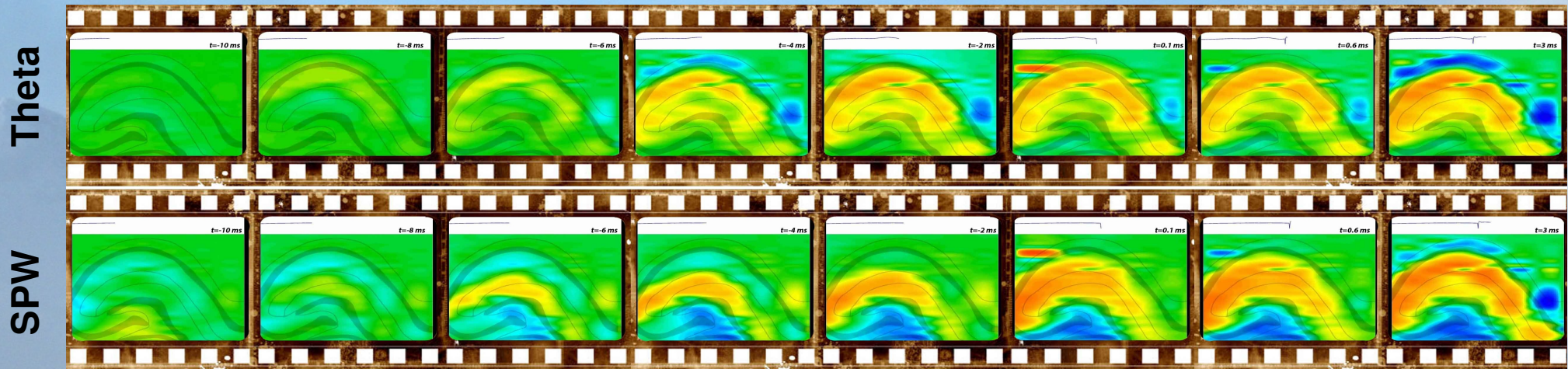
Micro-electro imaging

Micro-electro anatomy: 512 channel electrode system in the neocortex



Micro-electro imaging

Two inputs of one neuron



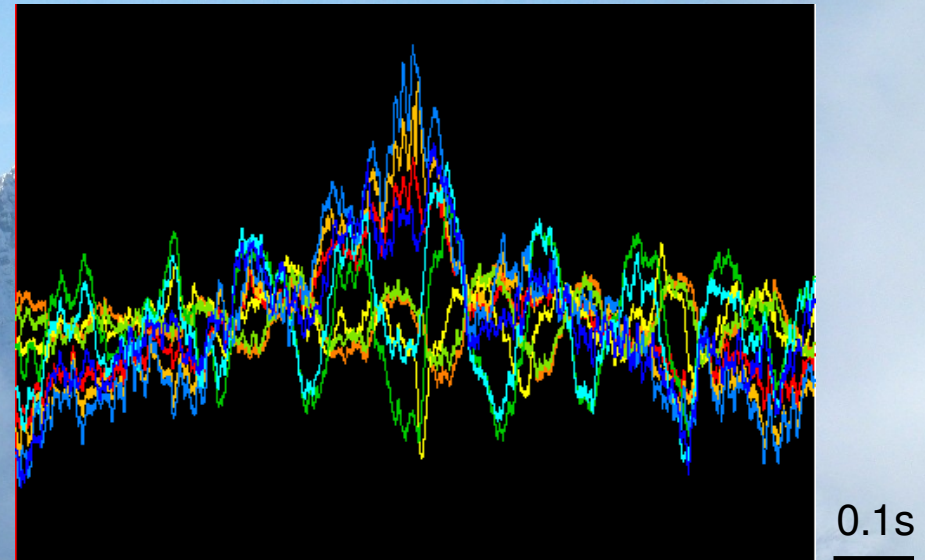
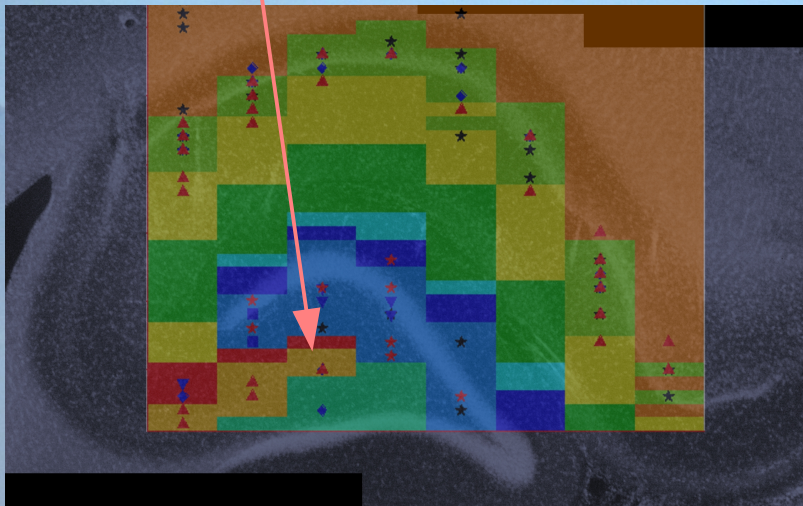
We have first demonstrated directly, that the same (inter)neuron receives synaptic inputs on different pathways during two different oscillatory (and information processing) stages of hippocampus.

Nat. Reviews Neurosci. 2012, 13(6) 407-20

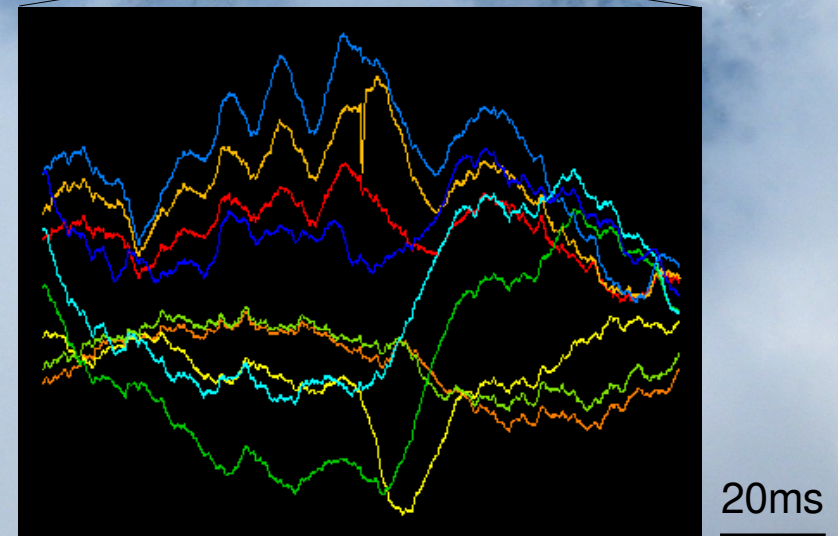
Micro-electro imaging

Inputs of a neurons from different layers

A CA3 pyramid neuron (#56)



The colors of the curves on the right show the spike triggered average EC potential of the corresponding cluster above. We can identify the EC signs of the input and the post-synaptic effect of the output as well.



Micro-electro imaging

István Ulbert, MTA TTK



Acknowledgement

György Buzsáki, NYU



**Antal Berényi, NYU
Szegedi Egyetem**



Lisa Roux, NYU



John Long, NYU



Micro-electro imaging

Acknowledgement

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Fülöp Bazzó

**László
Négyessy**



Dorottya Cserpán

László Zalányi

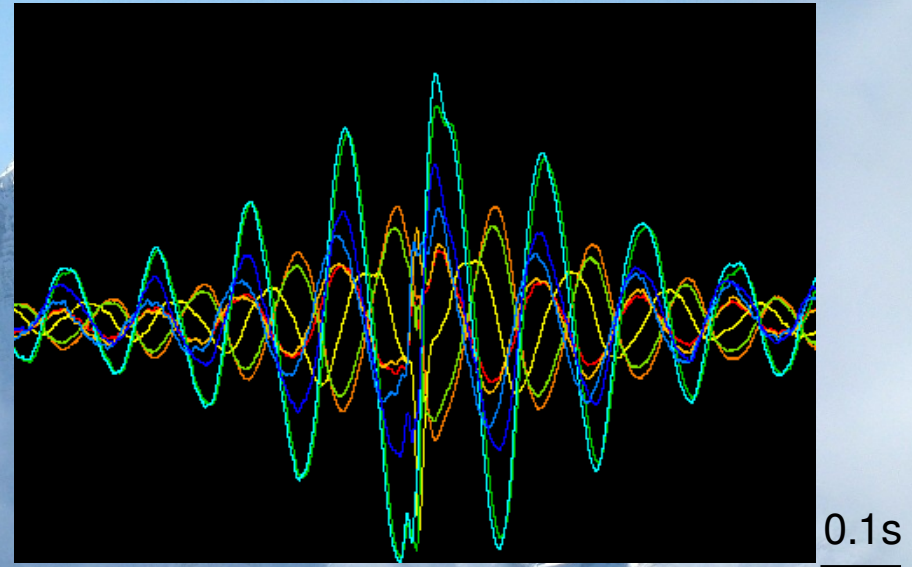
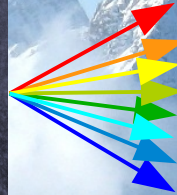
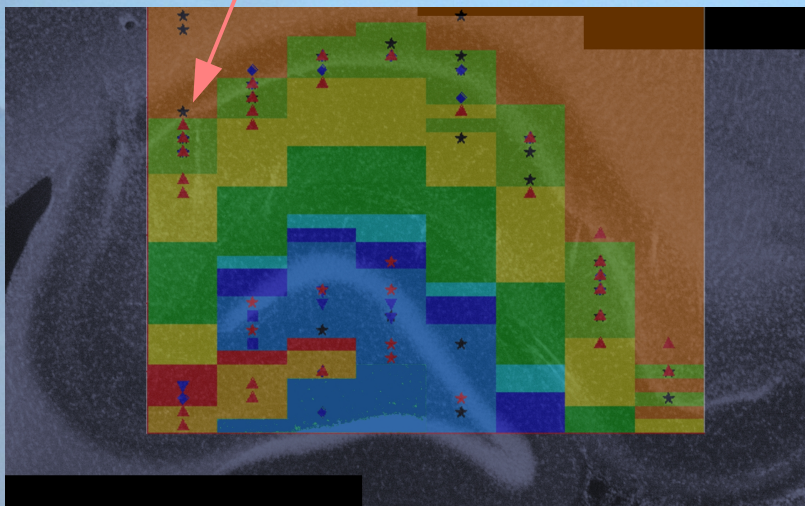
Zsigmond Benkő

Theoretical Neuroscience and Complex Systems Research Group

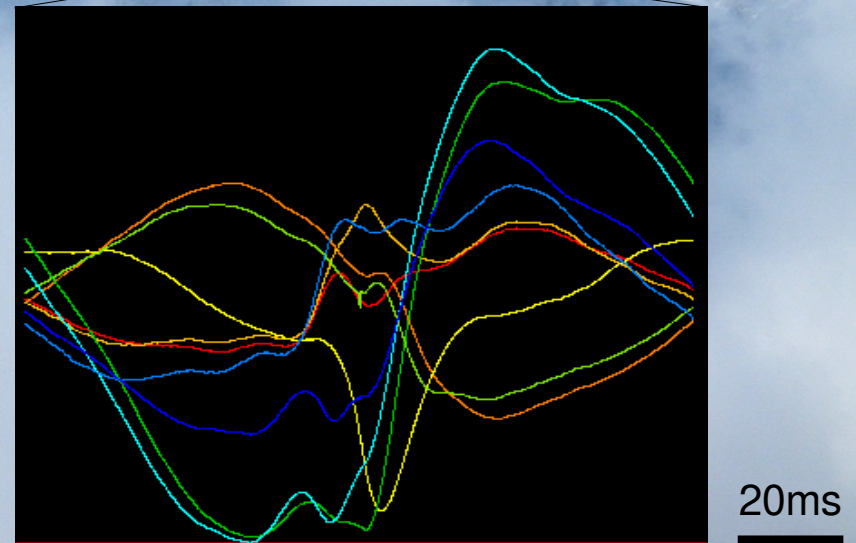
Micro-electro imaging

Inputs of a neurons from different layers

A CA1 interneuron (#8)



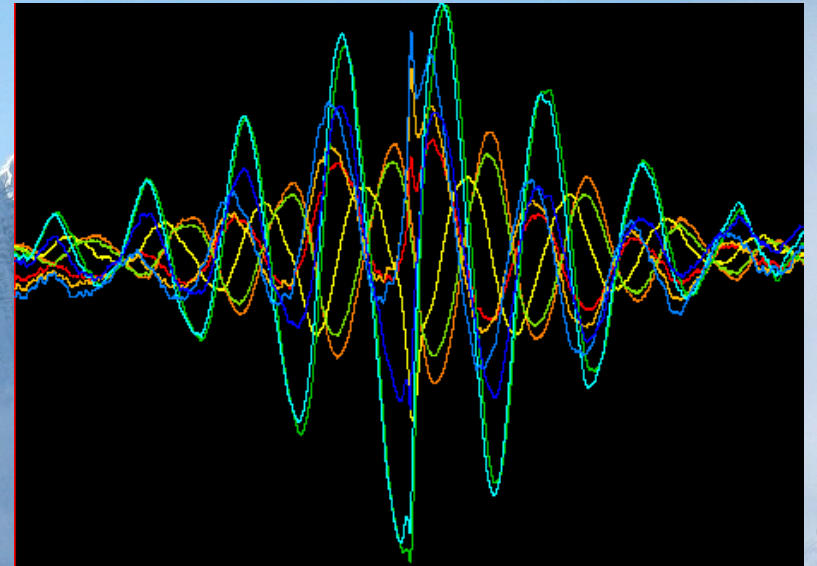
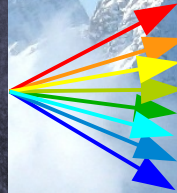
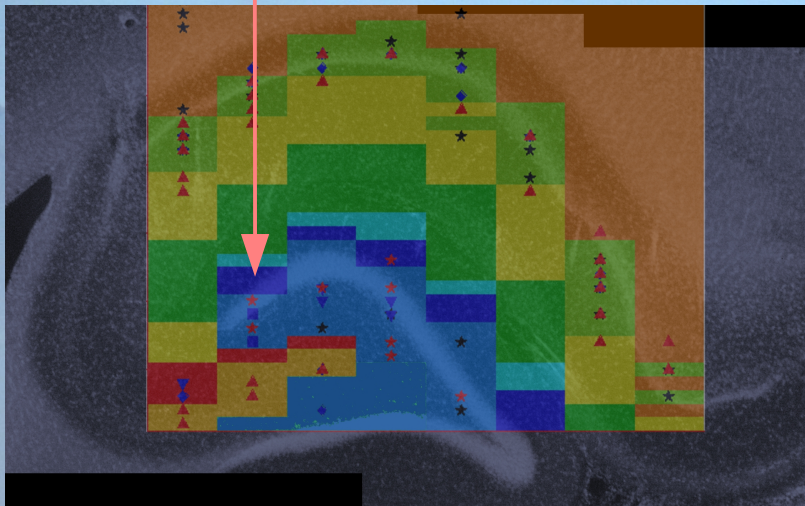
The colors of the curves on the right show the spike triggered average EC potential of the corresponding cluster above. We can identify the EC signs of the input and the post-synaptic effect of the output as well.



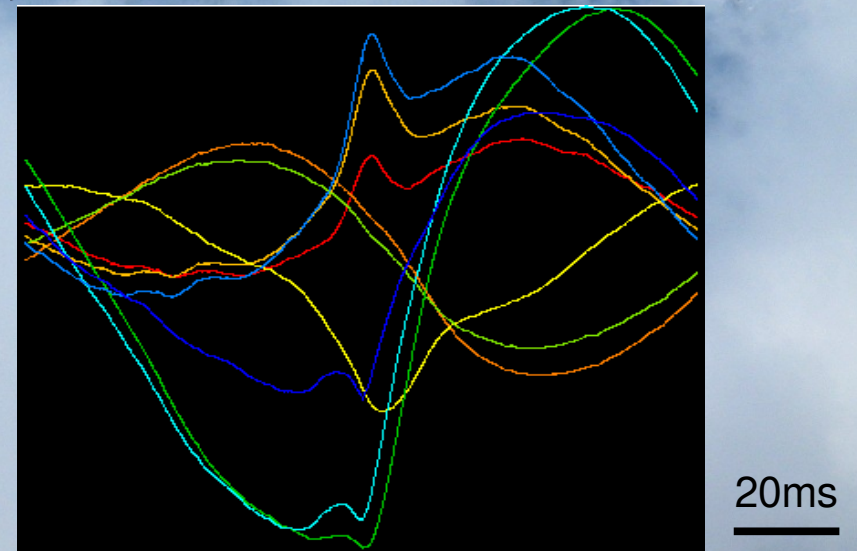
Micro-electro imaging

Inputs of a neurons from different layers

A DG neuron (#36)



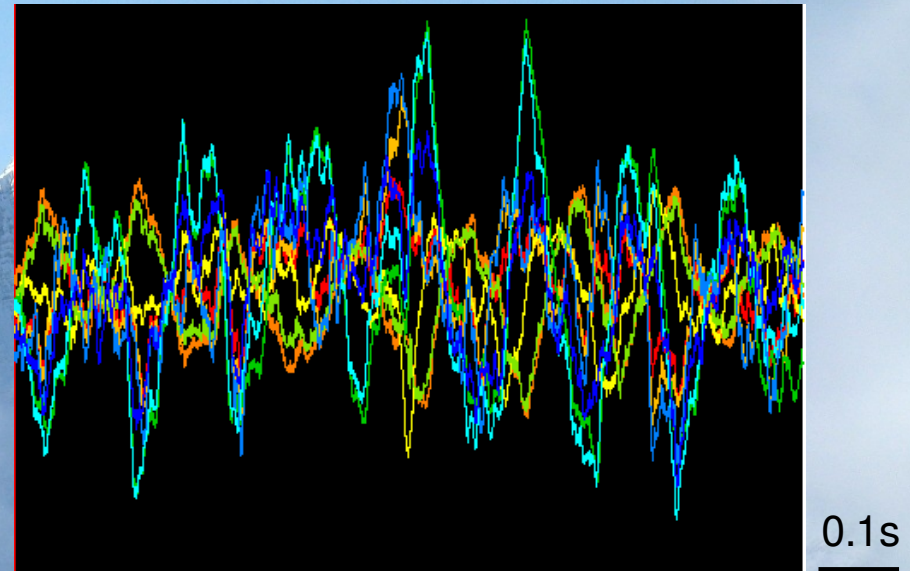
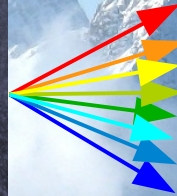
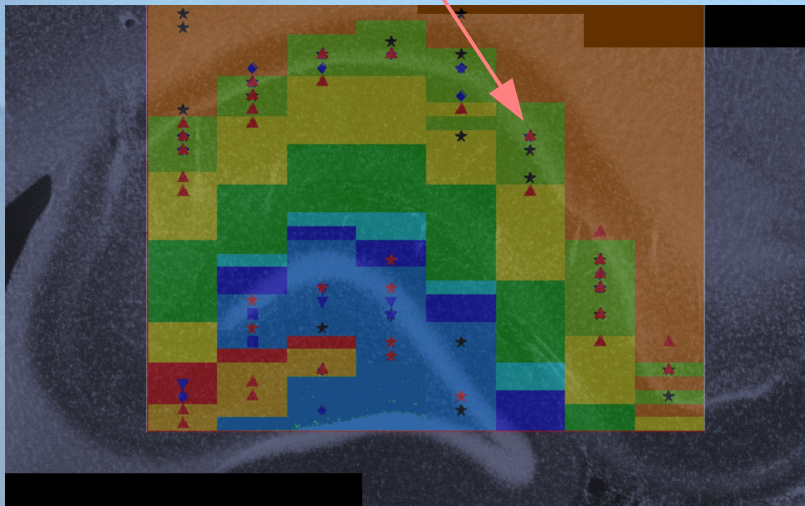
The colors of the curves on the right show the spike triggered average EC potential of the corresponding cluster above. We can identify the EC signs of the input and the post-synaptic effect of the output as well.



Micro-electro imaging

Inputs of a neurons from different layers

A CA1 pyramid neuron (#86)



The colors of the curves on the right show the spike triggered average EC potential of the corresponding cluster above. We can identify the EC signs of the input and the post-synaptic effect of the output as well.

